

Campus d'Excel·lència Internacional

grau Enginyeria Física

Graphene antennas for nanotechnology-enabled Wireless Communications

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Team and projects



- “Graphene-enabled Wireless Communications” funded by the **Samsung Advanced institute of Technology** (Seoul, Korea) under the GRO gift program
- “Graphene antennas for Wireless Networks-on-chip” funded by the **Intel research**
- EU FET flagship project “Graphene”
- EU FET flagship accesit “Guardian Angels”
- EU FET flagship project “Human Brain project”

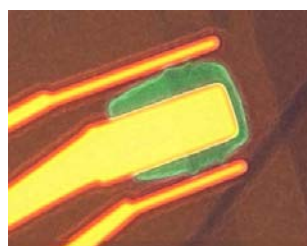
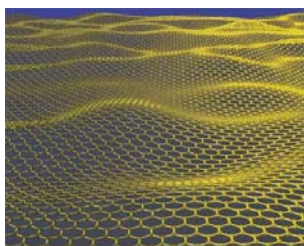
 <p>Dr. Albert Cabellos (AC)</p> 	 <p>Prof. Ian Akyildiz (UPC Hon.)</p> 
 <p>Ignacio Llatser</p> 	 <p>Dr. Mario Nemirovski</p> 
 <p>Josep Miquel Jornet (UPC, MIT)</p> 	 <p>Prof. Max Lemme</p> 
 <p>Prof. Eduard Alarcón (EE)</p> 	 <p>Prof. Tomas Palacios</p> 

Grafè



● Grafè

- Capa de carboni monoatòmic (d'un sol àtom de gruix)
- Xarxa cristal·lina en forma de niu d'abella
- Descobert per A. K. Geim i K. S. Novoselov el 2004
- Aquest descobriment els va valer el premi Nobel de física



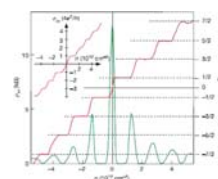
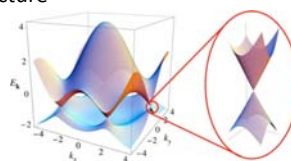
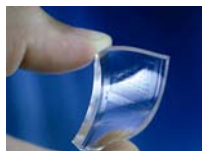
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Grafè



● Quines són les propietats extraordinàries del grafè que han atret l'atenció d'investigadors al voltant del món?

- Material més fi i lleuger observat a la natura (0.3 nanometers)
- Més dur que el diamant
- 300 cops més resistent que l'acer (Young modulus 1 TPa (Steel \sim 0.2 TPa))
- Condueix l'electricitat molt millor que el coure
- Transparent (97.7% optical transparency)
- Flexible: pot prendre qualsevol forma
- One-atom-thick impermeable membrane
- Gapless energy band structure



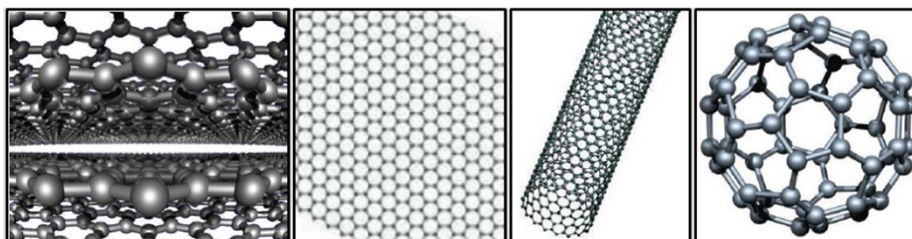
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Production of Graphene



Graphene in many dimensions

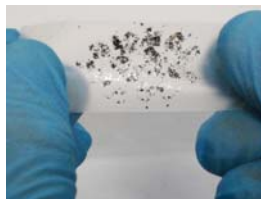
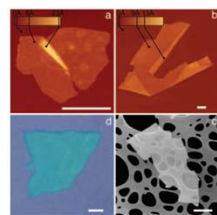
- 3D in graphite
- 2D in single layer (graphene)
- 1D in carbon nanotubes
- 0D in fullerenes



Anton Lopatin, Graphene a new Electronic Material FAU Erlangen-Nürnberg

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Graphene Mechanical Exfoliation




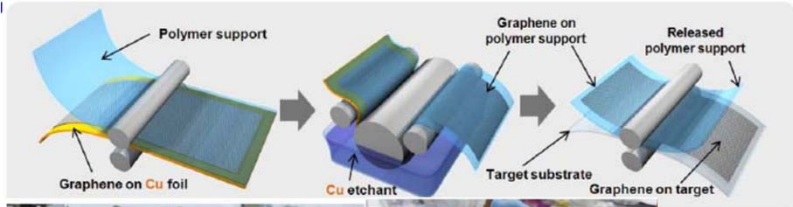
- Graphene flakes were preliminary identified with optical microscope
- Analysis with Atomic Force Microscopy
- Before it was believed that they could not exist due to thermal instability
- *“The found class of 2D crystals offers a wide choice of new materials parameters for possible applications and promises a wealth of new phenomena usually abundant in 2D systems.”*


K. S. Novoselov, D. Jiang, F. Schedin, T. J. Booth, V. V. Khotkevich, S. V. Morozov, and A. K. Geim “Two-dimensional atomic crystals” Proceedings of the National Academy of Sciences of the USA 2005

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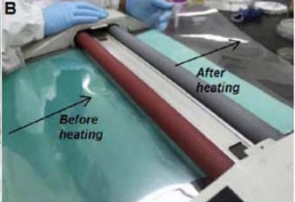
Production of large Graphene sheets








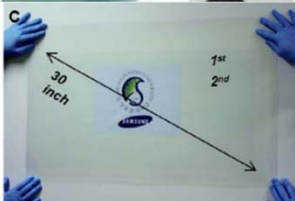
A



B



C




D

**SKKU Process
Bae Nature Nano (2010)**

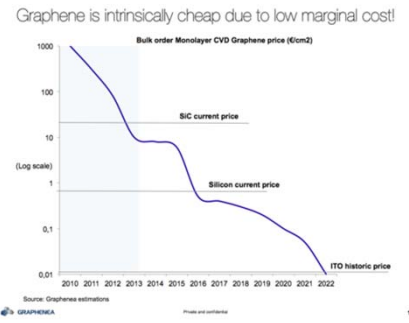
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Mass production of graphene



- Graphite is cheap (\$ per kg)
- Graphene cost is related to its quality (e.g. electron mobility)
 - Graphene oxide
 - CVD Graphene
 - Mechanically exfoliated graphene
- According to the estimates graphene cost is expected to decrease

Graphene is intrinsically cheap due to low marginal cost!




Source: Graphenea estimations
© GRAPHENEA Prices and estimates

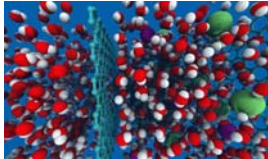
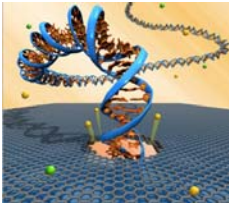
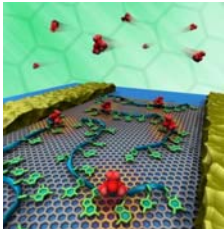
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Marko Spasenovic "The Price of Graphene" Graphenea 2011


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Grafè 

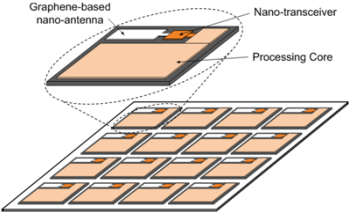
- Aquestes propietats fan del grafè possibiliten avenços disruptius en múltiples àmbits de la ciència i la tecnologia:
 - **Materials**
 - Pantalles tàctils resistents i flexibles
 - Estructures resistents i lleugeres (aeronàutica)
 - **Química**
 - Sensors de gasos ultra-precisos
 - Neteja d'aigua contaminada per material radioactiu
 - Destil·lació d'alcohol a temperatura ambient
 - Dessalinització d'aigua
 - **Bio-medicina**
 - Detecció de bacteris
 - Seqüenciació de l'ADN

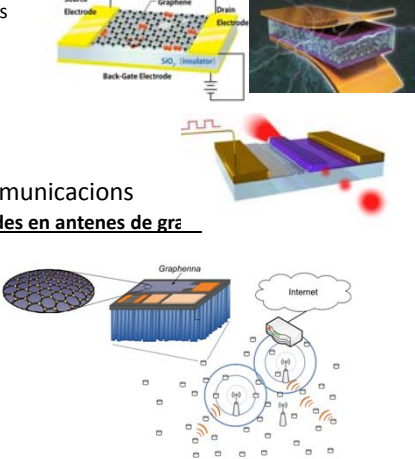
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Grafè 

- **Nano-electrònica**
 - Transistors i circuits integrats ultra-ràpids
 - Super-condensadors (bateries)
 - Efecte piezoelèctric a la nano-escala
- **Nano-òptica**
 - Nano-làsers
 - Moduladors òptics
- **Tecnologies de la informació i les comunicacions**
 - Comunicacions de rang ultra-curt basades en antenes de grafè



Mid-term: Graphene-based Wireless Network-on-Chip for Multi-Core processors



Long-term: Wireless Nano-Sensor Networks (WNSN)

I. F. Akyildiz, J. M. Jornet, "The Internet of Nano-Things", IEEE Wireless Communications, 2010.
 S. Abadal, A. Cabellos-Aparicio, J. A. Lázaro, E. Alarcón, J. Solé-Pareta, "Graphene-enabled hybrid architectures for multiprocessors: bridging nanophotonics and nanoscale wireless communication," in Proc. of the International Conference in Transparent Optical Networks (ICTON), 2012.

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Graphene Electronic Properties



- Graphene is a semi-metal or a zero-gap semiconductor
- Very high mobility for electrons: $20.000 \text{ cm}^2\text{V}^{-1}\text{s}^{-1}$ (Si $1400 \text{ cm}^2\text{V}^{-1}\text{s}^{-1}$)
 - An orders of magnitude better than Si
 - Best conductor yet discovered
- Electrons behave as massless Dirac fermions
- Very low scattering
- Very low resistivity $10^{-6} \Omega\cdot\text{cm}$
- Lowest material at room temperature
- Graphene can help to obtain faster and smaller electronics

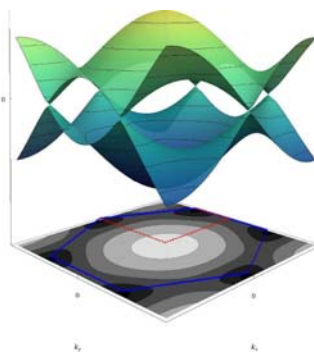
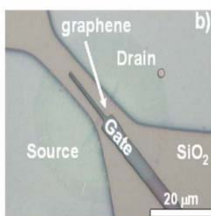
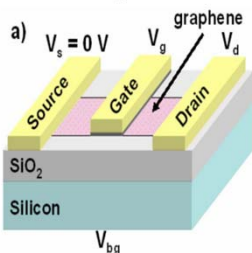
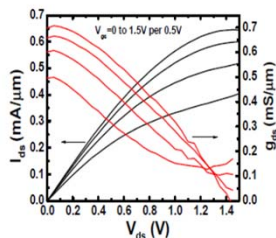


Image: Graphenea

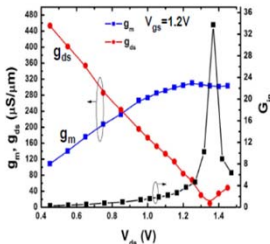
Graphene High-Frequency Transistors: Field-Effect T.



- Exfoliated graphene => No mass-production
- SiO₂ substrate => Mobility degraded
- No gate alignment => High access resistance
- Metal-Graphene junction => High contact-resistance

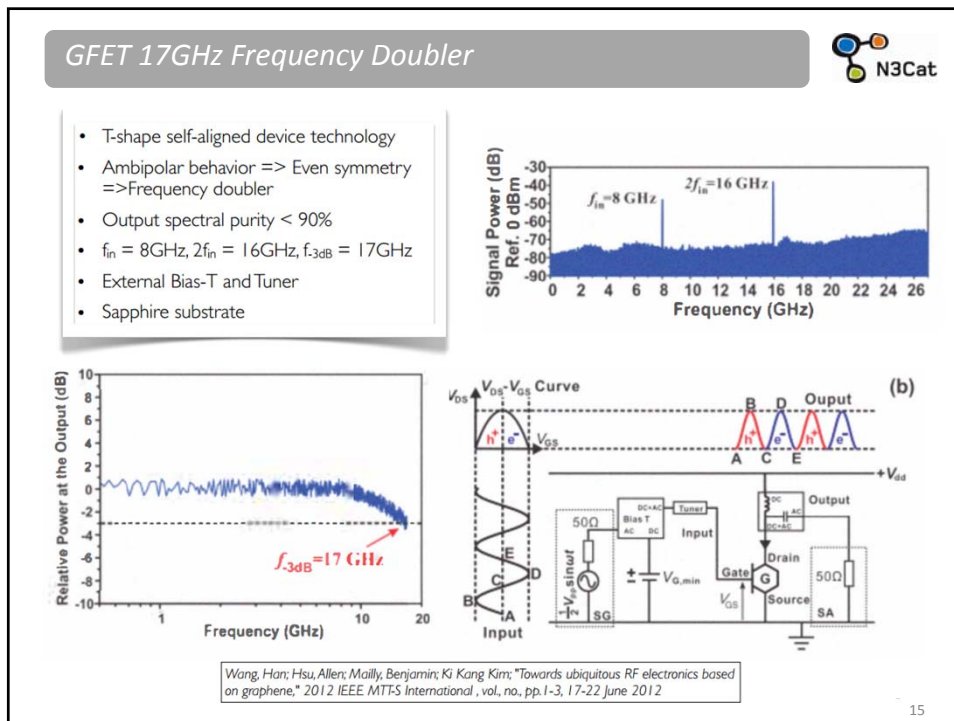
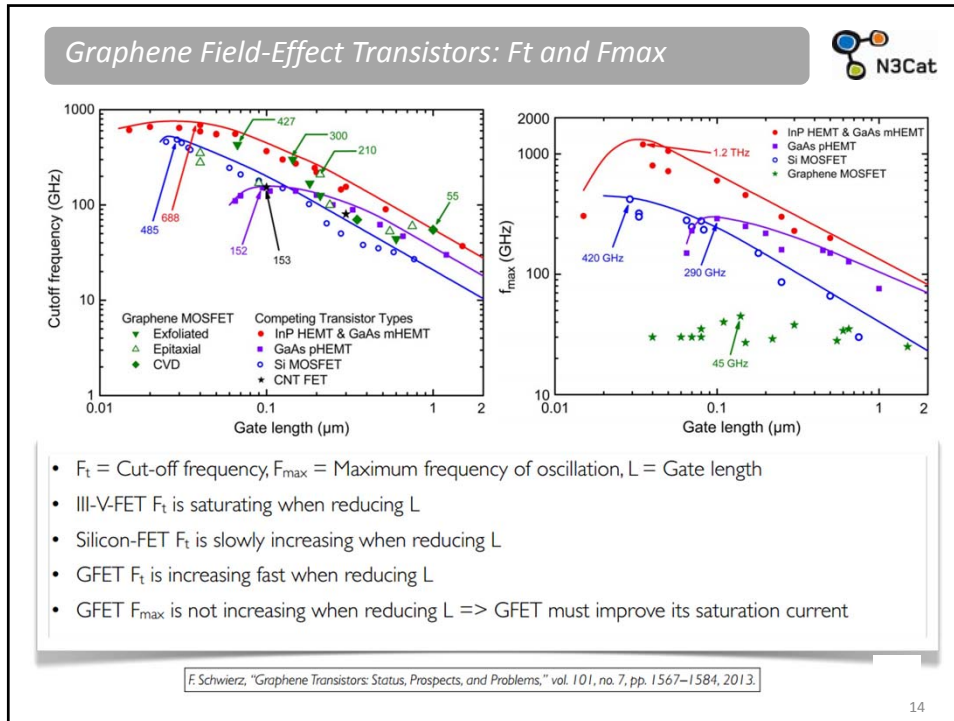


M. Lemme, "Current status of graphene transistors," Solid State Phenomena, pp. 1–11, 2010.




C-Y. Sung, "Near 400 GHz World Fastest Graphene RF Transistor For High Frequency Nanoelectronics and Circuits CMOS Platform Integration", Graphene Conference 2012

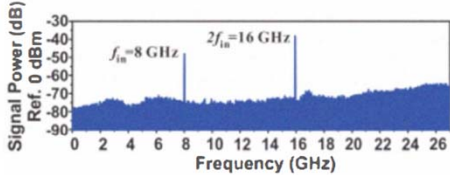
- CVD and Epitaxial GFET => Mass production
- Diamond-like carbon- substrate => Mobility improved
- Ultrathin gate-dielectric => Current-saturation improvement
- L_{ch}=40nm => f_r=350GHz



GFET 17GHz Frequency Doubler

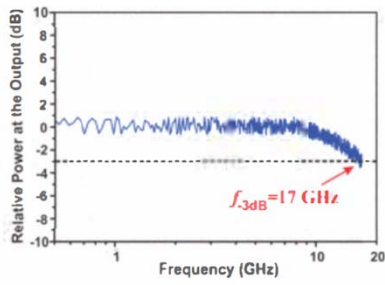
- T-shape self-aligned device technology
- Ambipolar behavior => Even symmetry => Frequency doubler
- Output spectral purity < 90%
- $f_{in} = 8\text{GHz}$, $2f_{in} = 16\text{GHz}$, $f_{3dB} = 17\text{GHz}$
- External Bias-T and Tuner
- Sapphire substrate





Signal Power (dB)
Ref. 0 dBm

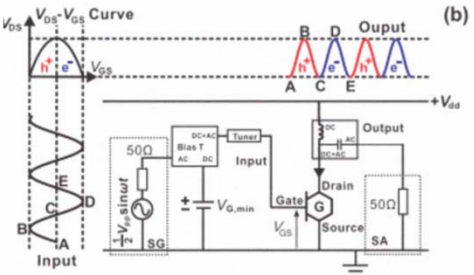
Frequency (GHz)



Relative Power at the Output (dB)

Frequency (GHz)

$f_{3dB} = 17\text{ GHz}$




(b)

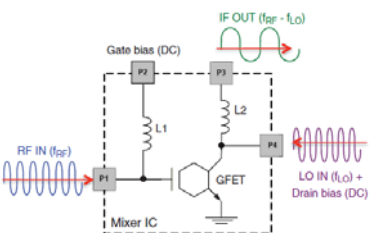
Wang, Han; Hsu, Allen; Maily, Benjamin; Ki Kang Kim; "Towards ubiquitous RF electronics based on graphene," 2012 IEEE MTT-S International, vol., no., pp.1-3, 17-22 June 2012

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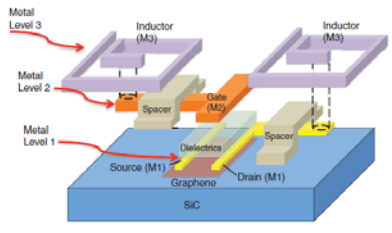
Experimental measurements of graphene devices

- Wafer-scale graphene integrated circuit
 - Broadband RF mixer at frequencies up to 10 GHz
 - Including a graphene FET and inductors

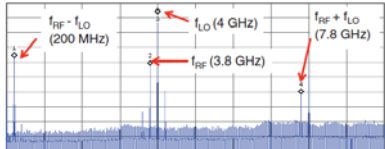




Mixer IC



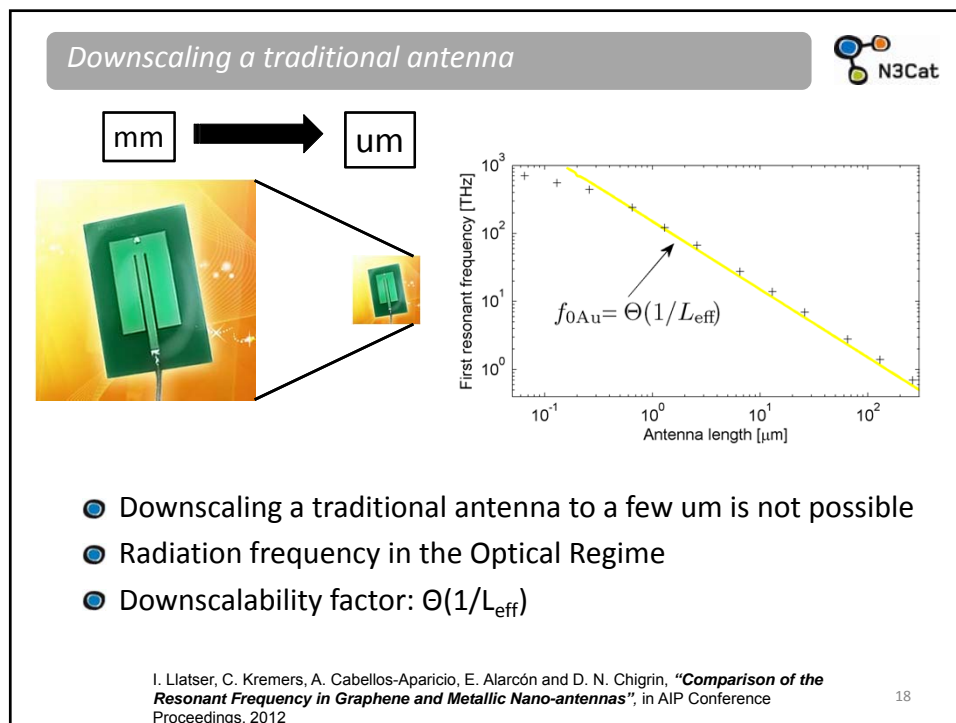
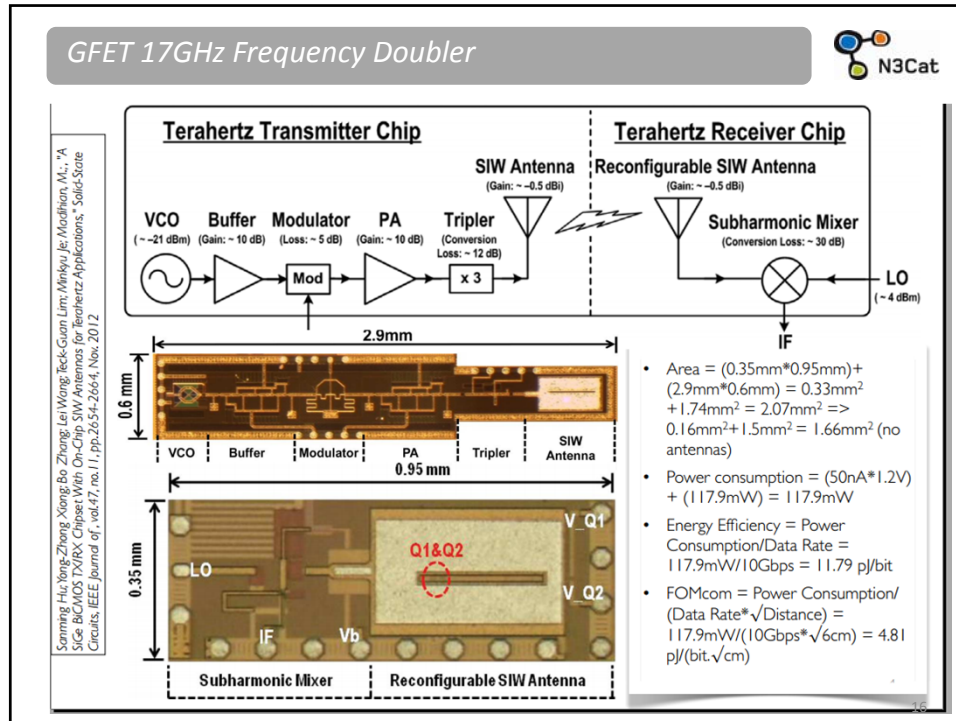
SiC



$f_{RF} - f_{LO}$ (200 MHz)
 f_{LO} (4 GHz)
 f_{RF} (3.8 GHz)
 $f_{RF} + f_{LO}$ (7.8 GHz)

Y. Lin, A. Valdes-Garcia, S. Han, D. B. Farmer, I. Meric, Y. Sun, Y. Wu, C. Dimitrakopoulos, A. Grill, P. Avouris and K. A. Jenkins, "Wafer-Scale Graphene Integrated Circuit", Science, 2014 (IBM)

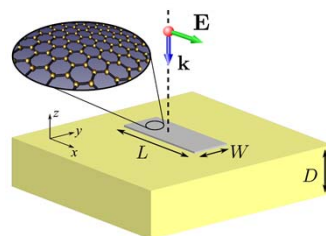
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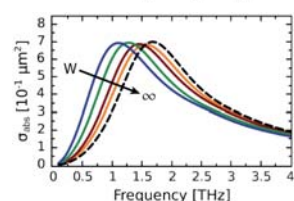
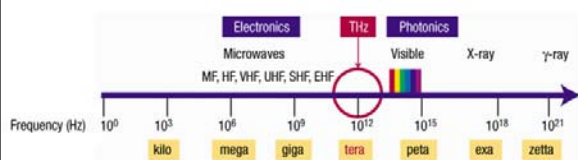
Graphene antennas at THz band



- Explore antennas that resonate
 - much lower frequency than optical regime
 - High end of the EM RF band
- Graphene-based plasmonic nano-antennas (graphennas)
 - Size in the μm range
 - Predicted to radiate in the THz band



$$\sigma(\omega) = \frac{2e^2 k_B T}{\pi \hbar} \ln \left[2 \cosh \left[\frac{\mu_c}{2k_B T} \right] \right] \frac{i}{\omega + i\tau^{-1}}$$



- EU FET flagship project "Graphene"

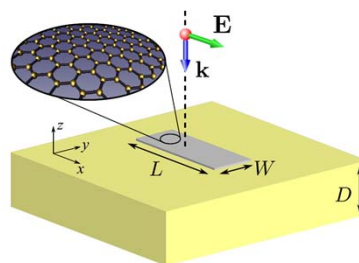


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Graphene-enabled Wireless Communications



- **Graphene-enabled Wireless Communications (GWC)** advocate for the use of graphene RF plasmonic antennas, or **graphennas**, to communicate nanosystems
- The working principle of graphennas is as follows
 - When an EM wave irradiates the antenna, it excites the free electrons on the graphene layer
 - Surface Plasmon Polariton (SPP) waves propagate at the interface between the graphene layer and the dielectric material
 - The generated SPP waves resonate in the antenna edges

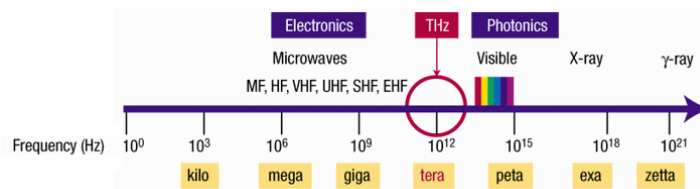


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Graphene-enabled Wireless Communications



- Graphene plasmonic antennas can be developed by exploiting the propagation of SPP waves in the graphene
- The novelty of graphennas is that they propagate SPP waves in the **terahertz band** (0.1 – 10 THz)
- Up to two orders of magnitude below metallic plasmonic antennas
- Comparable radiation efficiency
- Wide tunability

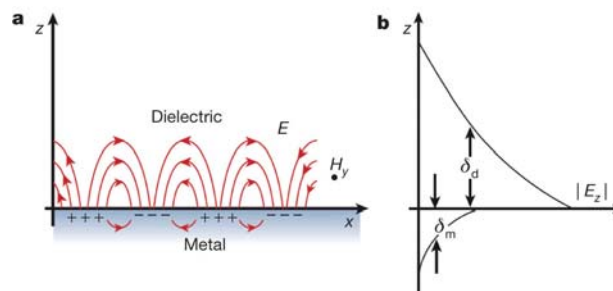


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Analysis of graphene RF plasmonic antennas



- In order to understand the behavior of graphennas, we need to study the propagation of **Surface Plasmon Polariton (SPP)** waves in graphene
 - EM waves guided along a metal-dielectric interface which are generated by an incident high-frequency radiation



O. Benson, "Assembly of hybrid photonic architectures from nanophotonic constituents", *Nature*, 2011.

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Analysis of graphene RF plasmonic antennas



- Current plasmonic nano-antennas
 - Made of noble metals (gold, silver)
 - Typical size ~ 10-100 nm
 - Resonant wavelength ~ 1 μm (frequency ~ 100 THz)
- Such a high frequency is not appropriate for omnidirectional wireless communications
- However, graphene has the potential to resonate in the terahertz band
 - Graphene is able to propagate SPP waves at much lower frequencies than metallic antennas
 - Expected frequency range for future ultra-fast integrated circuits

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Analysis of graphene RF plasmonic antennas



- In order to calculate the resonant frequency of graphene, we consider their **dispersion relation**
 - Relates the wavenumber with the frequency of SPP waves propagating in a graphene layer

$$\frac{1}{\sqrt{k_{\text{SPP}}^2 - \frac{\omega^2}{c^2}}} + \frac{\varepsilon}{\sqrt{k_{\text{SPP}}^2 - \varepsilon \frac{\omega^2}{c^2}}} = -i \frac{\sigma(\omega)}{\omega \varepsilon_0}$$

ε : dielectric constant of the substrate
 ε_0 : dielectric constant of vacuum
 β : wavenumber
 ω : angular frequency
 c : speed of light
 $\sigma(\omega)$: conductivity of graphene

$$n_{\text{eff}}(\omega) = \sqrt{1 - 4 \frac{\mu_0}{\varepsilon_0} \frac{1}{\sigma(\omega)^2}}$$

The graphene conductivity will determine the properties of SPP in graphene

Marinko Jablan, Hrvoje Buljan and Marin Soljačić, "Plasmonics in graphene at infrared frequencies" PHYSICAL REVIEW B 80, 245435 2009 (MIT)

Analysis of graphene RF plasmonic antennas



- The frequency-dependent **electrical conductivity** of a graphene monolayer is obtained using the random-phase approximation

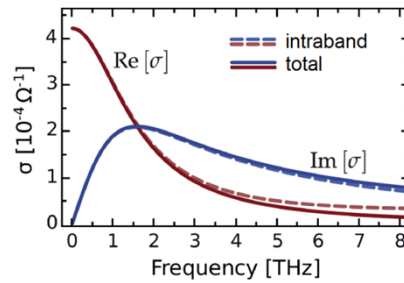
$$\sigma(\omega) = \frac{2e^2}{\pi\hbar} \frac{k_B T}{\hbar} \ln \left[2 \cosh \left[\frac{\mu_c}{2k_B T} \right] \right] \frac{i}{\omega + i\tau^{-1}} \quad \text{intradband contribution}$$

$$\sigma_i(\omega) = \frac{e^2}{4\hbar} \left(H\left(\frac{\omega}{2}\right) + i \frac{4\omega}{\pi} \int_0^\infty d\epsilon \frac{H(\epsilon) - H(\omega/2)}{\omega^2 - 4\epsilon^2} \right)$$

$$H(\epsilon) = \frac{\sinh(\hbar\epsilon/k_B T)}{\cosh(\mu_c/k_B T) + \cosh(\hbar\epsilon/k_B T)}$$

$\sigma(\omega)$: conductivity of graphene
 ω : angular frequency
 e : electron charge
 \hbar : reduced Planck's constant
 k_B : Boltzmann's constant
 T : temperature
 μ_c : chemical potential
 τ : relaxation time

interband contribution



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Analysis of graphene RF plasmonic antennas

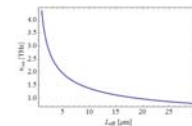


- The graphene patch acts as a Fabry-Perot resonator for SPP waves with the resonance condition

$$(1) \quad L = L' + 2\delta L = m \frac{\lambda_{SPP}}{2} = m \frac{\pi}{k_{SPP}} \quad \begin{array}{l} L: \text{effective antenna length} \\ k_{SPP}: \text{SPP wavenumber} \\ \lambda_{SPP}: \text{SPP wavelength} \\ m: \text{resonance order} \end{array}$$

- By combining the resonance condition (1) with the dispersion relation in graphene (2), we can obtain the resonant frequency of graphene antennas as a function of their length

$$(2) \quad \frac{1}{\sqrt{k_{SPP}^2 - \frac{\omega^2}{c^2}}} + \frac{\epsilon}{\sqrt{k_{SPP}^2 - \epsilon \frac{\omega^2}{c^2}}} = -i \frac{\sigma(\omega)}{\omega \epsilon_0}$$



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Analysis of graphene RF plasmonic antennas



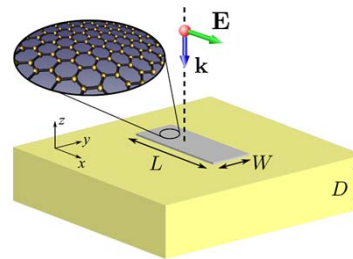
- The resonant frequency of graphennas can also be obtained by means of FEM electromagnetic simulations
 - Solve Maxwell's equations numerically with the appropriate boundary conditions
- An incident plane wave normally incident to the antenna is considered

$$\oint \mathbf{E} \cdot d\mathbf{A} = \frac{Q}{\epsilon_0}$$

$$\oint \mathbf{B} \cdot d\mathbf{A} = 0$$

$$\oint \mathbf{E} \cdot d\mathbf{s} = -\frac{d\Phi_m}{dt}$$

$$\oint \mathbf{B} \cdot d\mathbf{s} = \mu_0 I + \epsilon_0 \mu_0 \frac{d\Phi_e}{dt}$$

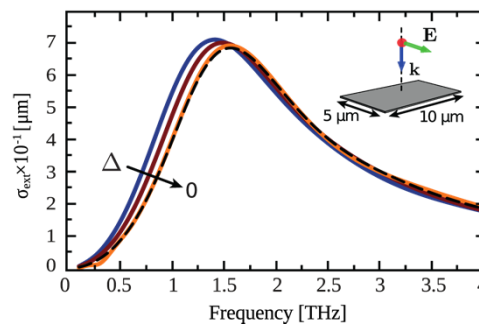


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Analysis of graphene RF plasmonic antennas



- Two graphenna models are considered
 - Thin slab of graphene with a finite thickness
 - Normalized effective conductivity σ/Δ
 - High mesh density \rightarrow high computational cost
 - Graphene sheet as an equivalent surface impedance $Z_s=1/\sigma$
 - Current in graphene is purely superficial
 - Much lower computational cost

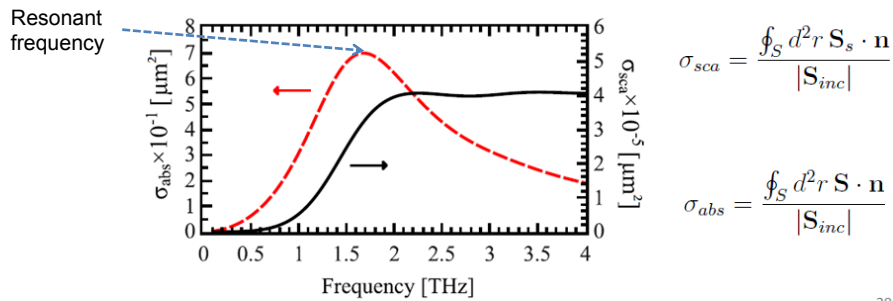


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Analysis of graphene RF plasmonic antennas



- The scattering and absorption cross sections of the graphenna are numerically calculated
 - As expected in nanostructures, absorption (red line) is several orders of magnitude higher than scattering (black line)
- The **resonant frequency** is obtained as the frequency at which the absorption cross section is maximized

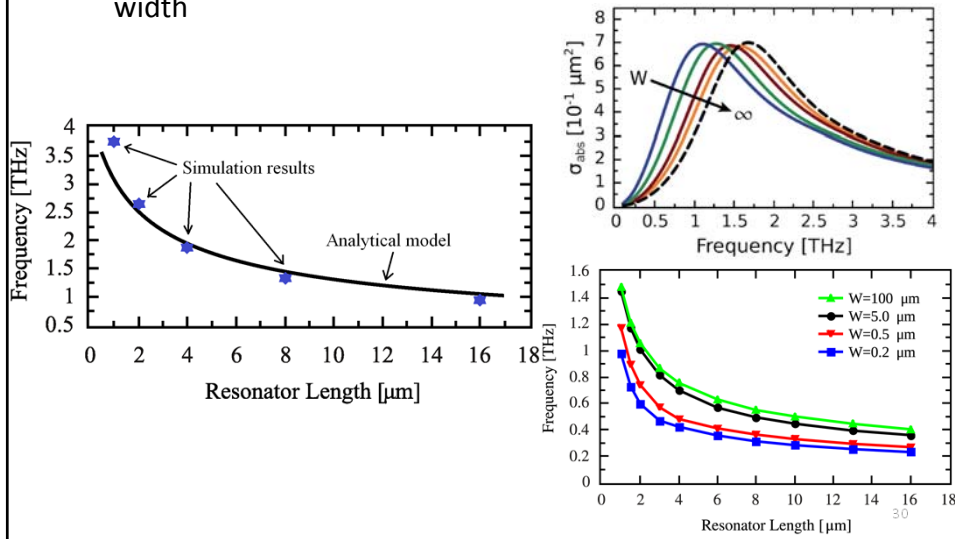


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Tunability of the resonant frequency in graphennas



- Antenna resonant frequency as a function of its length and width



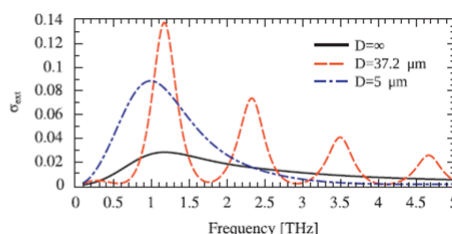
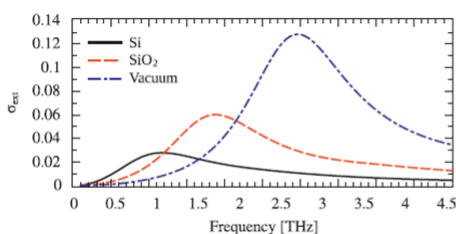
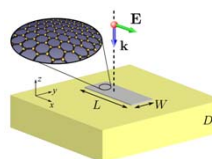
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Tunability of the resonant frequency in graphennas



● Influence of varying the substrate material and thickness

- The resonant frequency decreases when ϵ_r increases
- By adjusting the substrate thickness, a larger resonance can be achieved



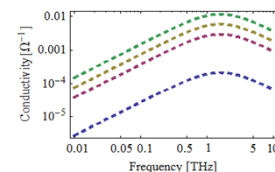
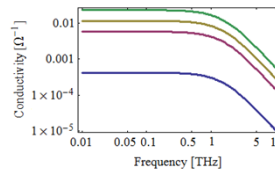
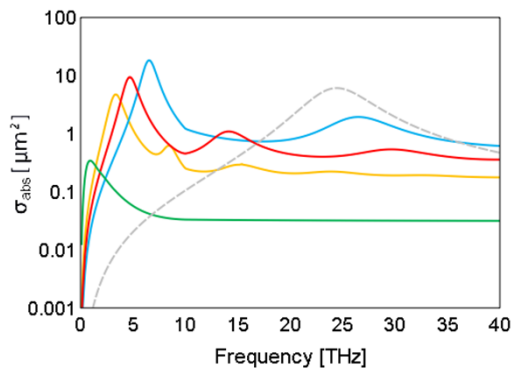
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Tunability of the resonant frequency in graphennas



● The resonant frequency of graphennas can be tuned by changing the chemical potential

- This can be achieved by chemical doping of the graphene layer or by applying an electrostatic bias



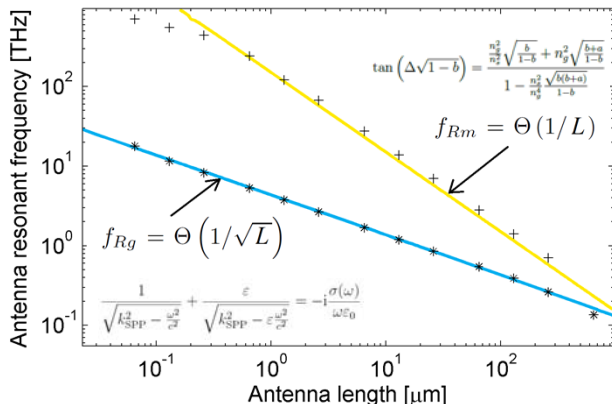
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Comparison of graphennas and metallic antennas



Scalability of the resonant frequency in graphennas and metallic antennas

- Graphennas resonate not just at a lower frequency, but they also scale better with respect to the antenna size than metallic antennas!



Graphennas with a size of a few μm resonate in the terahertz band, 1 to 2 orders of magnitude lower than metallic antennas!

yellow line: metallic antennas
blue line: graphennas
crosses: simulation results

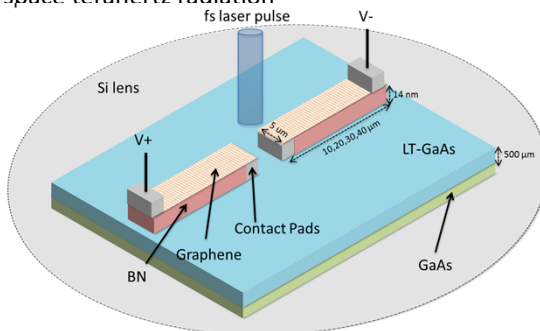
I. Llatser, C. Kremers, A. Cabellos-Aparicio, J. M. Jornet, E. Alarcón and D. N. Chigrin, "Graphene-based Nano-patch Antenna for Terahertz Radiation", Photonics and Nanostructures - Fundamentals and Applications, May 2012.

Photoconductive-fed graphennas



A practical technique to feed graphennas is by means of photoconductive sources

- Laser radiation excites photocarriers in the biased semiconductor and generates terahertz pulses
- The excitation of SPP waves in the dipole graphene produces a free-space terahertz radiation



A. Cabellos-Aparicio, I. Llatser, E. Alarcón, A. Hsu and T. Palacios, "Use of THz Photoconductive Sources to Characterize Graphene RF Plasmonic Antennas", IEEE Transactions on Nanotechnology (UPC / MIT)

Photoconductive-fed graphennas



- A model of the photoconductive antenna allows deriving the voltage of the generated terahertz pulses
 - The power radiated by the graphenna is obtained by considering the antenna impedance, radiation efficiency and mismatch loss pulses

$$\frac{dn(t)}{dt} = -\frac{n(t)}{\tau_c} + G(t)$$

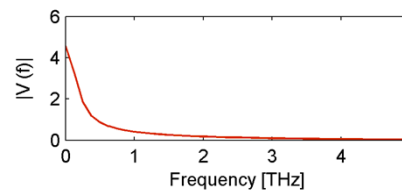
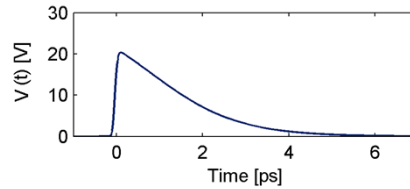
$$\frac{dv(t)}{dt} = -\frac{v(t)}{\tau_s} + \frac{e}{m} E_{loc}$$

$$\frac{dP_{sc}(t)}{dt} = -\frac{P_{sc}(t)}{\tau_r} + j(t)$$

$$V(t) = Z_a \cdot j(t) \beta \cdot V_c(t)$$

$$P = V^2 / Z_a$$

$$P_{rad} = M_L \cdot \epsilon_R \cdot P$$

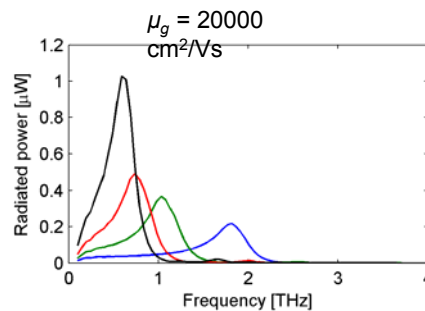
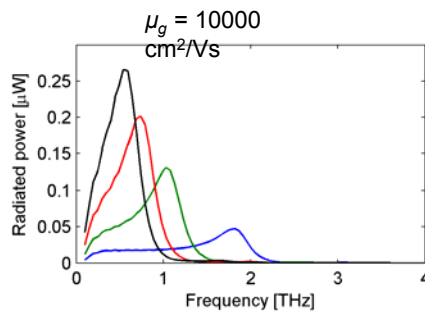
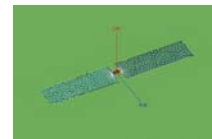


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Photoconductive-fed graphennas



- Power radiated by the photoconductive graphenna, for different antenna lengths
 - Frequency content in the terahertz band
 - Increases with the electron mobility in graphene

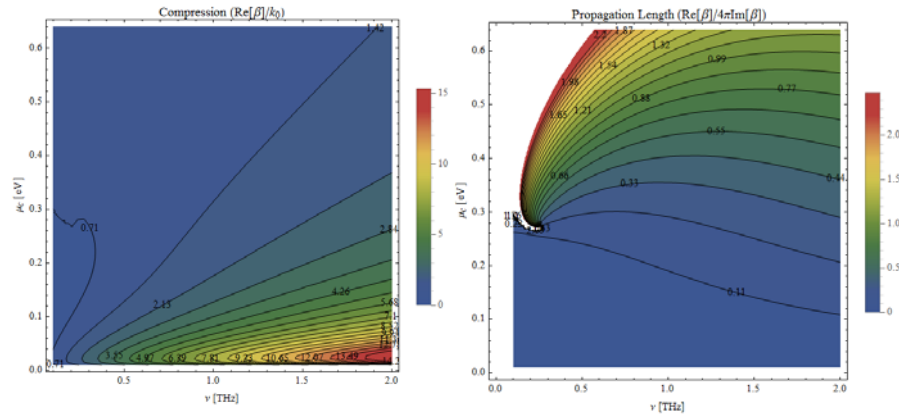


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Operational range of graphene antennas



- How graphene antennas downscalability advantage compares to metallic antennas?



A. Cabellos, I. Llatser, E. Alarcón, A. Hsu, and T. Palacios, Max Lemme, Mikael Östling
 B. (UPC / MIT / KTH / Ericsson)

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Application 1: wireless multicore processors



- Computer performance improvement is no longer achievable by simply increasing the operation frequency

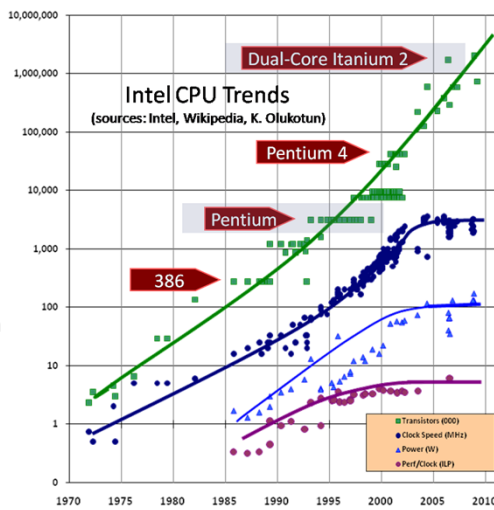
- Heat
- Power consumption
- Current leakage

Emergence of manycore processors

- The performance bottleneck of multicore processors has shifted from clock frequency to inter-core communication capabilities.

- Need of new scalable communication techniques

Comms Network-on-Chip (NoC)



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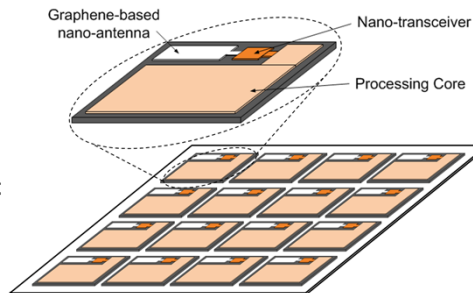
Graphene-enabled Hybrid Optical/Wireless NoC (II)



Graphene microantennas for wireless Network-on-Chip architectures

WHY WIRELESS for NOC?

- Multi-user shared RF medium
- Latency
- Reconfigurability
- Inherent broadcast and multicast
- 3D FFT supercomputers and
- Big Data (Google)



PhD Candidate Sergi Abadal "Intel Doctoral Student Award"
"Graphene-enabled Wireless Communications for Manycore Architectures"



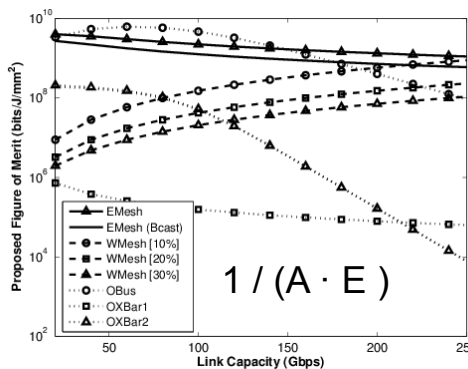
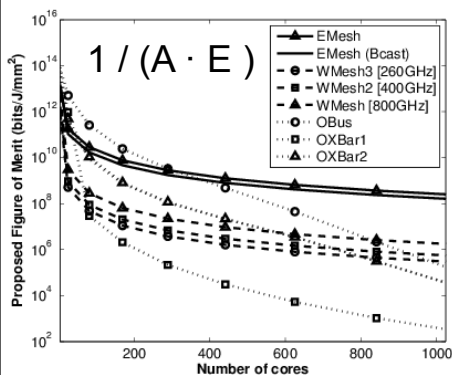
● EU FET flagship project "Human Brain project"

GWNoC: Feasibility Study



● Implementation-Communications

- How do area (A) and bit energy (E) scale?



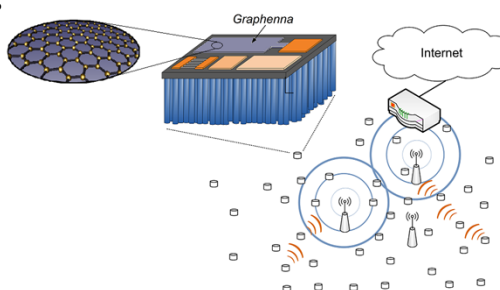
S. Abadal, M. Iannazzo, M. Nemirovsky, A. Cabellos-Aparicio, H. Lee, E. Alarcón, "On the Area and Energy Scalability of Wireless Network-on-Chip: A Model-based Benchmarked Design Space Exploration", submitted for publication on IEEE Transactions on Networking, Oct. 2013, revision in process.

Aplicació 2: xarxes de nano-sensors sense fils



● Nano-sensor

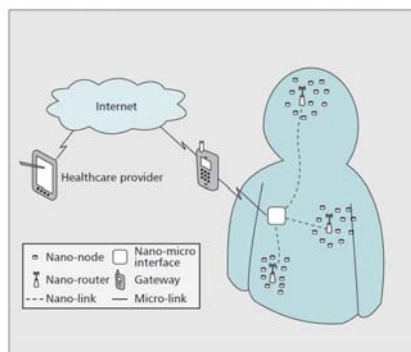
- Nanodispositius d'una dimensió de uns quants (pocs) micròmetres
- Capacitat de mesurar, processar i emmagatzemar informació
- I de recol·lectar l'energia que necessita per sensar i processar (*energy harvesting*), per exemple amb nanofils de zinc
- Equipats amb antenes de grafè per comunicar-se (via ràdio) amb d'altres nano-sensors



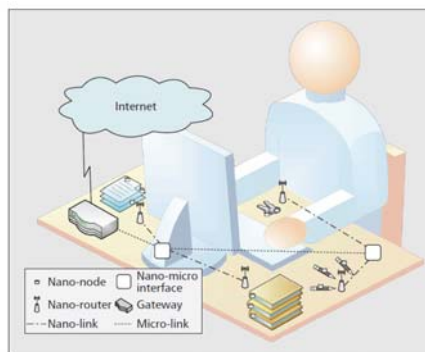
Aplicació 2: xarxes de nano-sensors sense fils



● Algunes aplicacions de les xarxes de nano-sensors:



Sistema de detecció de malalties i administració cooperativa de medicaments (Intrabody networks)



Internet de les nano-coses (Internet of nano-things)

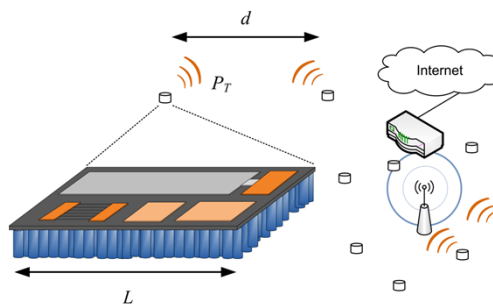
● EU FET flagship project "Guardian Angels"



Channel capacity in GWC



- The scalability of the channel capacity in GWC is studied as a function of three scale parameters
 - Antenna length L
 - Transmission distance d
 - Transmitted power P_T
- The results using graphennas and metallic antennas are compared



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Channel capacity in GWC



- The channel capacity is obtained with the Shannon-Hartley theorem, integrated over the whole terahertz band

$$C = \max_{S(f): \int_B S(f) df \leq P_T} \int_B \log_2 \left(1 + \frac{S(f)}{A(f)N(f)} \right) df$$

Transmitted power spectral density

$$S(f) = \begin{cases} P_T/B & \text{if } 0 < f < B, \\ 0 & \text{otherwise.} \end{cases}$$

Noise power spectral density

$$N(f, d) = k_B(T_{sys} + T_{mol}(f, d))$$

$$T_{mol}(f, d) = T_0(1 - e^{-k(f)d})$$

$$T_{sys} = T_0 = 293 \text{ K}$$

Channel attenuation

$$A = A_{spread} A_{abs}$$

$$A_{spread} = \left(\frac{4\pi f d}{c} \right)^2$$

$$A_{abs} = \frac{1}{\tau_m} = e^{k(f)d}$$

Bandwidth

$$B_m = \frac{k_1}{L} \quad B_g = \frac{k_2}{\sqrt{L}}$$

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Channel capacity in GWC



● Expression of the channel capacity in GWC

- The factor P_T/d^2 will have a key role

$$C(B, d, P_T) = \int_0^B \log_2 \left(1 + \frac{P_T/B}{\left(\frac{4\pi f d}{c}\right)^2 N_0} \right) df$$

$$= \frac{B}{\log 2} \log \left(1 + \frac{c^2 P_T}{(4\pi d)^2 B^3 N_0} \right) + \frac{c\sqrt{P_T}}{2 \log(2) \pi d \sqrt{N_0 B}} \arctan \frac{4\pi d B^{3/2} \sqrt{N_0}}{c\sqrt{P_T}}$$

$$C_m(L, d, P_T) = \frac{k_1}{\log(2)L} \log \left(1 + \frac{c^2 L^3 P_T/d^2}{(4\pi)^2 N_0 k_1^3} \right) + \frac{c\sqrt{L P_T/d^2}}{2 \log(2) \pi \sqrt{N_0 k_1}} \arctan \frac{4\pi \sqrt{N_0 k_1^3}}{c\sqrt{L^3 P_T/d^2}}$$

$$C_g(L, d, P_T) = \frac{k_2}{\log(2)\sqrt{L}} \log \left(1 + \frac{c^2 L^{3/2} P_T/d^2}{(4\pi)^2 N_0 k_2^3} \right) + \frac{c\sqrt[4]{L} \sqrt{P_T/d^2}}{2 \log(2) \pi \sqrt{N_0 k_2}} \arctan \frac{4\pi \sqrt{N_0 k_2^3}}{c L^{3/4} \sqrt{P_T/d^2}}$$

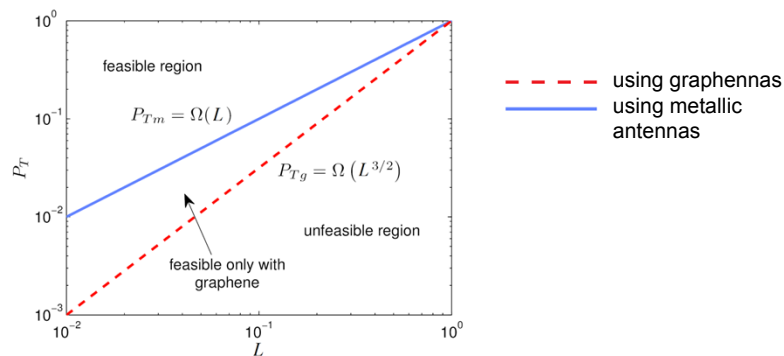
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Channel capacity in GWC



● Scalability of the transmitted power in GWC with respect to the antenna length

- Additional feasibility condition: the network shrinks proportionally
 - Transmission distance scales proportionally to the antenna length ($\alpha=1$)
- Graphennas require less power than metallic antennas as their size is reduced to the nanoscale



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Thanks



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