

# ELECTROMAGNETISM

## PART A) Electrostatics and magnetostatics with dielectric and magnetic materials

(0) Introduction: microscopic fields produced by charges and spins vs classical field theory

### **(1) Summary and extension of electrostatics**

(1.1) Electrostatic field (**E**), charge density ( $\rho$ ), electrostatic potential ( $V$ ): Coulomb, Gauss, and Poisson's laws

(1.2) Electric dipole (**p**): potential and field of the point dipole; induced and permanent dipoles, torque and energy of a permanent electric dipole under an applied field

(1.3) Special dipole distributions: the line dipole and the sphere dipole; multipole expansion for  $V$  (and  $E$ )

(1.4) Electrostatic properties of metals, surface charge density ( $\sigma$ ), boundary conditions for  $E$  at a metal surface

(1.5) Uniqueness theorem: capacitance ( $C$ ) and electrostatic energy; image charge method

### **(2) Dielectric materials**

(2.1) Polarization field (**P**), bound charge density;  $E$ -field of polarized dielectrics (depolarizing field)

(2.2) Linear dielectrics vs ferroelectric materials (electrets); electric susceptibility & macroscopic electric field in linear dielectrics

(2.3) Electric displacement field (**D**); dielectric constant and capacitance of capacitors with dielectrics

(2.4) Boundary conditions for  $E$  and  $D$ ; relationships between free, bound and total charge densities

(2.5) Electrostatic energy with linear dielectrics and calculation of electric forces in capacitors

(2.6) Microscopic description of linear media (Clausius-Mossotti relation) and of ferroelectrics

### **(3) Magnetic materials and magnetic field**

(3.1) Spin and magnetic moment (**m**); dipolar magnetic field, Coulomb's law for magnetism; torque and energy of a permanent magnetic dipole under an applied field

(3.2) Magnetization field (**M**), magnetic poles and pole densities; auxiliary field (**H**) for magnetized media

(3.3) Linear materials: magnetic susceptibility and permeability, paramagnetism and diamagnetism; demagnetizing  $H$ -field, macroscopic  $H$  and  $B$  fields; saturation magnetization

(3.4) Maxwell's equations for magnetostatics without free currents, boundary conditions for  $H$  and  $B$

(3.5) Microscopic description of permanent magnets: exchange interactions, magnetic domains; soft and hard ferromagnetic materials

### **(4) Summary and extension of electric currents and magnetism**

(4.1) Electric current ( $I$ ) & current densities (**J**, **K**); charge conservation; free and bound currents

(4.2) Ohm's local law: dc conductivity ( $g$ ), classification of materials; generation of steady currents

(4.3) Calculations of resistance ( $R$ ); Joule's law;  $R$ - $C$  relation in homogeneous media; charge densities at boundaries between media

(4.4) Magnetic field due to free currents: Biot-Savart's and Ampère's laws for  $B$

(4.5) Free currents near and inside linear magnetic media: Ampère law for  $H$ ; magnetic circuits, reluctance, Hopkinson's law

(4.6) Ampère's equivalence theorem, equivalent currents; multipole expansion; magnetic dipole of a current loop

(4.7) Superconductivity and superconducting currents

## PART B) Time-varying fields, electromagnetic energy and waves, optical phenomena

### **(5) Magnetic energy & forces, Maxwell's equations, electromagnetic waves**

(5.1) Lorentz force and electromotive force; Faraday's law of induction

(5.2) Energy stored in the  $B$ -field, self-inductance ( $L$ ), magnetic energy in linear materials

(5.3) Magnetic forces within solenoids and magnetic circuits

(5.4) Overview of electric technology: electromagnets, generators, transformers, electric motors

(5.5) Displacement current and macroscopic Maxwell's equations; quasi-static approximations

(5.6) Poynting's vector (**S**) and Poynting's theorem; electromagnetic wave equations and speed of light in vacuum; monochromatic waves, irradiance, vacuum wavelength & electromagnetic spectrum

(5.7) Speed of light in perfect dielectrics, refractive index; boundary conditions: constancy of the frequency, Snell's law of refraction; reflectivity for normal incidence

### **(6) Description and propagation of electromagnetic (e.m.) waves in vacuum, metals and dielectrics**

(6.1) Complex notation for planar, spherical, and cylindrical e.m. waves; application to spatial & temporal interference: standing waves, phase velocity vs group velocity

(6.2) Attenuation of e.m. waves in lossy media: complex conductivity ( $\tilde{\sigma}$ ), complex dielectric function ( $\tilde{\epsilon}$ ), and complex refractive index ( $\tilde{n}$ ); skin depth; macroscopic model for  $\tilde{\epsilon}$  and  $\tilde{n}$

(6.3) Drude theory for metals, collisionless plasma model; current relaxation and frequency-dependent resistance

(6.4) Electromagnetic properties of dielectrics: Lorentz-Rayleigh model of the complex permittivity & refractive index of insulators; Rayleigh scattering; Debye model of the dipolar relaxation.

## Requirements

Participants must have passed the exams of the courses "Física 2" and "Càlcul 2". They should have attended some lectures on complex numbers.

## Evaluation system

The students' evaluation will consist of a final exam (EF), a midterm exam (EP) towards the end of topic 4, and an evaluation of handed-in homework (TE). The final mark will be given by:

$$\text{Max}\{\text{EF} ; 0.9*\text{EF} + 0.1*\text{TE} ; 0.55*\text{EF} + 0.35*\text{EP} + 0.1*\text{TE}\}$$

The students will also receive an English note (A to D), based on their knowledge of written (scientific) English, which will be evaluated based on the handed-in homework.

## Bibliography

*Textbook* : **Gerald Pollack, Daniel Stump, *Electromagnetism*, Pearson (2002)**

### *Other basic bibliography sources*

- J. R. Reitz, F. J. Milford, R. W. Christy, *Foundations of Electromagnetic Theory*, 4<sup>th</sup> Edition, Addison Wesley (2008)
- D. Griffiths, *Introduction to Electrodynamics*, 3<sup>rd</sup> Edition, Pearson (2003)
- Theory and problem-solving notes on Atenea

### *Complementary bibliography*

- A. Zangwill. *Modern Electrodynamics*. Cambridge University Press (2012)
- W. J. Duffin, *Electricity and magnetism*, 4<sup>th</sup> Edition, McGraw-Hill (1990)
- W. H. Hayt, Jr., y J. A. Buck. *Teoría electromagnética*, 8<sup>a</sup> Ed. Mc Graw Hill (2012)
- P. Lorrain, D. R. Corson, *Campos y ondas electromagnéticas*, 5<sup>a</sup> Ed., Selecciones Científicas (1990)
- R. K. Wangsness, *Campos electromagnéticos*, Limusa (2001)

### *"Informal" resources*

- Videlectures of the Electromagnetism course taught at MIT in 2002 by Prof. Walter Lewin:  
[https://www.youtube.com/playlist?list=PLUdYIQf0\\_sSsfcNOPSNPQKHDhSjTJATPu /](https://www.youtube.com/playlist?list=PLUdYIQf0_sSsfcNOPSNPQKHDhSjTJATPu/)
- J. Peatross, M. Ware, *Physics of Light and Optics*, 2011c edition, available at <http://optics.byu.edu/textbook.aspx>
- R. Feynman, R. B. Leighton, M. Sands, *The Feynman Lectures on Physics*, Vol 1 and 2, Addison Wesley (1964, latest edition in 2005)