# **SIGNAL THEORY**

Department: Signal Theory and Communications Lecturer in charge: Antonio Pascual Iserte Other lecturers: Javier Villares Piera, Francesc Rey Micolau Academic Period: 3A ECTS credits: 6

## **CONTENTS**

## 1. SIGNALS AND SYSTEMS IN THE TIME DOMAIN

- a. Analog and discrete-time signals. Basic signals. Energy and power.
- b. Analog and discrete-time systems. Examples (including transformations over the time variable) and properties/classification.
- c. Linear time invariant systems:
  - i. impulse response and convolution: properties
  - ii. differential equations for analog systems
  - iii. finite differences equations for discrete-time systems (FIR/IIR systems)

## 2. SIGNALS AND SYSTEMS IN TRANSFORM DOMAINS

- a. Analog signals and systems:
  - i. Fourier transform/series and frequency response (analog filters)
  - ii. examples and properties
- b. Discrete-time signals and systems:
  - i. Z transform and transfer function
  - ii. Fourier transform and frequency response (digital filters)
  - iii. DFT and FFT
  - iv. examples and properties

## 3. A/D AND D/A CONVERSION

- a. Sampling and alias generation: antialiasing filter.
- b. Change of the sampling frequency: decimation and interpolation.
- c. Signal reconstruction: ideal and zero-order hold (ZOH) interpolators.

## 4. STOCHASTIC PROCESSES – RANDOM SIGNALS

- a. Statistical characterization.
- b. Strict-sense and wide-sense stationary processes. Cyclo-stationary processes.
- c. Autocorrelation and power spectral density. Wiener-Khinchin theorem.
- d. Filtering of random signals.
- e. Gaussian processes.

## 5. FUNDAMENTALS OF ESTIMATION THEORY

- a. Introduction to estimation theory:
  - i. definition of estimator
  - ii. quality criteria: bias, variance, mean square error (MSE), consistency
  - iii. example: estimation of the mean of a process
- b. Classical estimation theory:
  - i. minimum variance unbiased estimator (MVUE)
  - ii. efficient estimators: Cramer-Rao bound
  - iii. maximum likelihood (ML) estimation
- c. Bayesian estimation theory:
  - i. parameter characterization: prior distribution
  - ii. Bayesian risk: maximum-a-posteriori (MAP), posterior mean

## 6. SPECTRAL ESTIMATION

- a. Non-parametric spectral estimation:
  - i. periodogram: bias (leakage), variance, and consistency
  - ii. smoothing the periodogram through windowing (Blackman-Tukey): Bartlett, Hamming, Kaiser, Blackman, etc.
  - iii. Bartlett-Welch spectral estimation techniques: average of periodograms
- b. Parametric spectral estimation:
  - i. linear models of processes: AR, MA, ARMA
  - ii. Yule-Walker equations

# 7. OPTIMAL WIENER FILTERING

- a. Linear Bayesian estimator of minimum MSE.
- b. Wiener filter and Wiener-Hopf equations.
- c. Adaptive implementation (steepest descent-SD, least mean square-LMS, normalized LMS-NLMS).
- d. Linear predictors. Examples.

# LAB SESSIONS

The course will contain around 5 lab sessions (2 hours each session and most of them using MATLAB) that will be carried out jointly by 2 students. The contents of the lab sessions will cover some concrete topics of the course and will be organized in groups of 20 students at most. The evaluation will be based on the previous work, the work performed during the session at class, the delivered reports, and/or some exam.

# **EVALUATION METHOD**

PE: partial examFE: final exam (including all the contents of the course)LS: lab sessions

Final mark = max { 0,60·FE + 0,25·PE + 0,15·LS , 0,85·FE + 0,15·LS }

Only when the final mark is not passed in the ordinary period, an extraordinary exam (**EE**) will be carried out including all the contents of the course. In this case, the final mark will be calculated as follows, where it is taken into account that the 15% corresponding to the lab sessions (LS) cannot be re-evaluated:

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Final mark = max { 0,60·FE + 0,25·PE + 0,15·LS , 0,85·FE + 0,15·LS , 0,85·EE + 0,15·LS }
```

## LANGUAGE

Material: all the material used in class will be in English Classes: Spanish, Catalan Previous work and lab reports: English, Spanish, Catalan

# **BIBLIOGRAPHY**

## **BASIC BIBLIOGRAPHY**

- Alan V. Oppenheim, Alan S. Willsky, S. Hamid Nawab, Signals and Systems. Ed. Prentice-Hall.
- Monson H. Hayes, Statistical Digital Signal Processing and Modeling. Ed. Wiley.
- Steven M. Kay, Fundamentals of Statistical Signal Processing: Estimation Theory. Ed. Prentice-Hall.

## COMPLEMENTARY/SPECIFIC BIBLIOGRAPHY

- Athanasios Papoulis, Probability, Random Variables, and Stochastic Processes. Ed. Mc-Graw-Hill.
- Dimitris G. Manolakis, Vinay K. Ingle, Stephen M. Kogon, *Statistical and Adaptive Signal Processing: Spectral Estimation, Signal Modeling, Adaptive Filtering, and Array Processing.* Ed. Artech House.
- John G. Proakis, Dimitris G. Manolakis, *Digital Signal Processing: Principles, Algorithms, and Applications.* Ed. Prentice-Hall.
- Simon Haykin, Barry Van Veen, Signals and Systems. Ed. Wiley.
- Alan V. Oppenheim, Ronald W. Schafer, Discrete-Time Signal Processing. Ed. Prentice-Hall.
- Louis L. Scharf, *Statistical Signal Processing: Detection, Estimation, and Time Series Analysis.* Ed. Addison-Wesley.