

IEEE AP
Levent Gürel
UPC Barcelona, Spain

ABAKUS

**Fast Algorithms and Parallel Computing:
Solution of Extremely Large Real-Life Problems
in Computational Electromagnetics**

Levent Gürel
CEO, ABAKUS Computing Technologies
Professor Emeritus, Bilkent University, Turkey
Founder, Computational Electromagnetics Research Center (BILCEM)
Adjunct Professor, Dept. of ECE, University of Illinois at Urbana-Champaign

www.abakus.computing.technology

IEEE AP
Levent Gürel
UPC Barcelona, Spain

ABAKUS

**Real-Life Electromagnetics Problems
At Different Frequencies**

100 MHz 100 GHz 100 THz

Antennas Photonic Crystals Metamaterials Biological Structures (RBC)

Indoor Propagation Wireless Communications Radar Systems THz-Range Circuits


Optical Imaging Systems

www.abakus.computing.technology

IEEE AP
Levent Gürel
UPC Barcelona, Spain

ABAKUS

Radars Problem

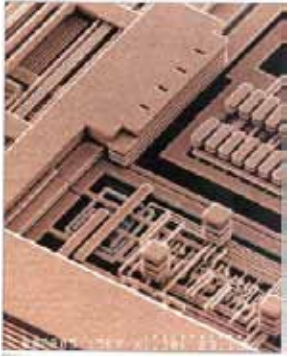


www.abakus.computing.technology

IEEE AP
Levent Gürel
UPC Barcelona, Spain

ABAKUS

**Real-Life Problem
Electromagnetic Modeling of Microcircuits**



www.abakus.computing.technology

IEEE AP
Lütfi Gürel
UPC Barcelona, Spain

ABAKUS

Application Examples: Photonics

Photonic crystals

Ö. Erçül, T. Malas, and L. Gürel, "Analysis of dielectric photonic-crystal problems with MLFMA and Schur-complement preconditioners," *J. Lightwave Technol.*, vol. 29, no. 6, pp. 888–897, Mar. 2011.

www.abakus.computing.technology

IEEE AP
Lütfi Gürel
UPC Barcelona, Spain

ABAKUS

Radiation into Living Organisms

www.abakus.computing.technology

IEEE AP
Lütfi Gürel
UPC Barcelona, Spain

ABAKUS

Microwave Imaging

www.abakus.computing.technology

IEEE AP
Lütfi Gürel
UPC Barcelona, Spain

ABAKUS

Antennas

www.abakus.computing.technology

IEEE AP
Lluís Górriz
UPC Barcelona, Spain

Mobile Device Antennas

ABAKUS

Bluetooth
Wi-Fi
GPS
UMTS
GSM

www.abakus.computing.technology

IEEE AP
Lluís Górriz
UPC Barcelona, Spain

Satellite Antennas

ABAKUS

www.abakus.computing.technology

IEEE AP
Lluís Górriz
UPC Barcelona, Spain

Antennas Mounted on Platforms

ABAKUS

- Interaction of multiple antennas
- Characteristics of mounted antennas (different from isolated antennas)
- Optimization of the placement of the antennas

www.abakus.computing.technology

IEEE AP
Lluís Górriz
UPC Barcelona, Spain

Simulation Environment

ABAKUS

```

graph TD
    ME[Maxwell's Equations] --> SIE[Surface Integral Equations]
    EMP[ELECTROMAGNETICS PROBLEMS] --> D[Discretization + Triangulation + Basis / Testing Functions]
    GM[Geometry Modelling] --> D
    SIE --> D
    D --> DME[Dense Matrix Equations]
    DME --> IM[Iterative Methods]
    MLFMA[Multilevel Fast Multipole Algorithm (MLFMA) Parallel Computers] --> IM
    P[Preconditioners] --> IM
    IM --> S[Solutions]
  
```

www.abakus.computing.technology

IEEE AP
Lluís Gómez
UPC Barcelona, Spain

ABAKUS

Maxwell's Equations

$$\nabla \times \bar{E}(\bar{r}, t) = -\frac{\partial}{\partial t} \bar{B}(\bar{r}, t)$$

$$\nabla \times \bar{H}(\bar{r}, t) = \frac{\partial}{\partial t} \bar{D}(\bar{r}, t) + \bar{J}(\bar{r}, t)$$

$$\nabla \cdot \bar{B}(\bar{r}, t) = 0$$

$$\nabla \cdot \bar{D}(\bar{r}, t) = \rho(\bar{r}, t)$$

www.abakus.computing.technology

IEEE AP
Lluís Gómez
UPC Barcelona, Spain

ABAKUS

Surface Integral Equations

- **Electric-Field Integral Equation (EFIE):**

$$-\hat{t}(\mathbf{r}) \cdot ik \int_{S'} d\mathbf{r}' \left(\bar{I} - \frac{\nabla \nabla'}{k^2} \right) g(\mathbf{r}, \mathbf{r}') \cdot \mathbf{J}(\mathbf{r}') = \frac{1}{\eta} \hat{t}(\mathbf{r}) \cdot \mathbf{E}^{inc}(\mathbf{r})$$
- **Magnetic-Field Integral Equation (MFIE):**

$$\mathbf{J}(\mathbf{r}) - \hat{n}(\mathbf{r}) \times \int_{S'} d\mathbf{r}' \mathbf{J}(\mathbf{r}') \times \nabla' g(\mathbf{r}, \mathbf{r}') = \hat{n}(\mathbf{r}) \times \mathbf{H}^{inc}(\mathbf{r})$$
- **Combined-Field Integral Equation (CFIE):**

$$CFIE = \alpha EFIE + (1 - \alpha) MFIE$$
- **Hybrid-Field Integral Equation (HFIE):**

$$HFIE = \alpha(\mathbf{r}) EFIE + [1 - \alpha(\mathbf{r})] MFIE$$

www.abakus.computing.technology

IEEE AP
Lluís Gómez
UPC Barcelona, Spain

ABAKUS

Geometry Discretization

Mesh Size: $\lambda/10$

www.abakus.computing.technology

IEEE AP
Lluís Gómez
UPC Barcelona, Spain

ABAKUS

Discretization

Number of unknowns

$$\mathbf{J}(\mathbf{r}) = \sum_{n=1}^N a_n \mathbf{b}_n(\mathbf{r})$$

• **Matrix equations:**

$$\sum_{n=1}^N Z_{mn}^{E,M,C,H} a_n = v_m^{E,M,C,H}, \quad m = 1, 2, \dots, N$$

• **Matrix elements:**

$$Z_{mn}^E = \int_{S_m} d\mathbf{r} \mathbf{t}_m(\mathbf{r}) \cdot \int_{S_n} d\mathbf{r}' \bar{\mathbf{G}}(\mathbf{r}, \mathbf{r}') \cdot \mathbf{b}_n(\mathbf{r}')$$

$$Z_{mn}^M = \int_{S_m} d\mathbf{r} \mathbf{t}_m(\mathbf{r}) \cdot \mathbf{b}_n(\mathbf{r}) - \int_{S_m} d\mathbf{r} \mathbf{t}_m(\mathbf{r}) \cdot \hat{n} \times \int_{S_n} d\mathbf{r}' \mathbf{b}_n(\mathbf{r}') \times \nabla' g(\mathbf{r}, \mathbf{r}')$$

$$Z_{mn}^C = \alpha Z_{mn}^E + (1 - \alpha) \frac{i}{k} Z_{mn}^M \quad Z_{mn}^H = \alpha_m Z_{mn}^E + (1 - \alpha_m) \frac{i}{k} Z_{mn}^M$$

www.abakus.computing.technology

IEEE AP
Lluís Górriz
UPC Barcelona, Spain

ABAKUS

Matrix Elements...

...are electromagnetic interactions

$$Z_{mn}^E = \int_{S_m} d\mathbf{r} \mathbf{t}_m(\mathbf{r}) \cdot \int_{S_n} d\mathbf{r}' \bar{\mathbf{G}}(\mathbf{r}, \mathbf{r}') \cdot \mathbf{b}_n(\mathbf{r}')$$

Testing functions Basis functions

$$\sum_{n=1}^N Z_{mn}^E a_n = v_m^E, \quad m = 1, 2, \dots, N$$

www.abakus.computing.technology

IEEE AP
Lluís Górriz
UPC Barcelona, Spain

ABAKUS

Geometry Discretization

Mesh Size: $\lambda/10$

Modeling with millions of triangles.

www.abakus.computing.technology

IEEE AP
Lluís Górriz
UPC Barcelona, Spain

ABAKUS

Matrix Equation

System of Linear Equations

$$\mathbf{A} \cdot \mathbf{x} = \mathbf{b}$$

$$\mathbf{Z} \cdot \mathbf{a} = \mathbf{v}$$

www.abakus.computing.technology

IEEE AP
Lluís Górriz
UPC Barcelona, Spain

ABAKUS

Two Equations with Two Unknowns

$$\begin{cases} x + y = 12 \\ 2x - 3y = 14 \end{cases}$$

www.abakus.computing.technology

IEEE AP
Lluís Gómez
UPC Barcelona, Spain

ABAKUS

Three Equations with Three Unknowns

$$\begin{cases} (a) 3x - 8y + z = -14 \\ (b) x - y + z = -5 \\ (c) x - 3y = -4 \end{cases}$$

www.abakus.computing.technology

IEEE AP
Lluís Gómez
UPC Barcelona, Spain

ABAKUS

Two Equations with Two Unknowns

$$\begin{cases} x + y = 12 \\ 2x - 3y = 14 \end{cases}$$

Cramer's Rule

$$x = \frac{\begin{vmatrix} 12 & 1 \\ 14 & -3 \end{vmatrix}}{\begin{vmatrix} 1 & 1 \\ 2 & -3 \end{vmatrix}} = \frac{12 \cdot (-3) - 1 \cdot 14}{1 \cdot (-3) - 1 \cdot 2} = \frac{-50}{-5} = 10$$

$$y = \frac{\begin{vmatrix} 1 & 12 \\ 2 & 14 \end{vmatrix}}{\begin{vmatrix} 1 & 1 \\ 2 & -3 \end{vmatrix}} = \frac{1 \cdot (14) - 12 \cdot 4}{1 \cdot (-3) - 1 \cdot 2} = \frac{-10}{-5} = 2$$

Solution: $x = 12 - y$, $y = 2$, $x = 12 - 2 = 10$

www.abakus.computing.technology

IEEE AP
Lluís Gómez
UPC Barcelona, Spain

ABAKUS

Three Equations with Three Unknowns

$$\begin{cases} 3x - 8y + z = -14 \\ x - y + z = -5 \\ x - 3y = -4 \end{cases}$$

Cramer's Rule

$$D = \begin{vmatrix} 3 & -8 & 1 \\ 1 & -1 & 1 \\ 1 & -3 & 0 \end{vmatrix} = 3 \cdot (-1) \cdot 0 + (-8) \cdot 1 \cdot 1 + 1 \cdot 1 \cdot (-3) - (-3 \cdot 1 \cdot (-3) - (-8) \cdot 1 \cdot 0 - 1 \cdot (-1) \cdot 1) = -1$$

Two Equations with Two Unknowns

$$D_x = \frac{\begin{vmatrix} -14 & 1 \\ -5 & 1 \end{vmatrix}}{D} = \frac{(-14) \cdot 1 - (-5) \cdot 1}{-1} = \frac{-14 + 5}{-1} = \frac{-9}{-1} = 9$$

$$D_y = \frac{\begin{vmatrix} -14 & 1 \\ -5 & 1 \end{vmatrix}}{D} = \frac{(-14) \cdot 1 - (-5) \cdot 1}{-1} = \frac{-9}{-1} = 9$$

$$D_z = \frac{\begin{vmatrix} 3 & -8 \\ 1 & -1 \end{vmatrix}}{D} = \frac{3 \cdot (-1) - (-8) \cdot 1}{-1} = \frac{-3 + 8}{-1} = \frac{5}{-1} = -5$$

www.abakus.computing.technology

IEEE AP
Lluís Gómez
UPC Barcelona, Spain

ABAKUS

Matrix Equation

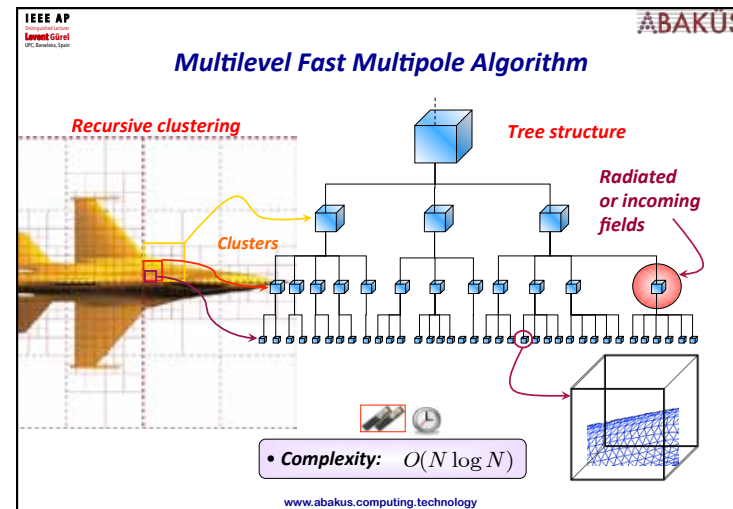
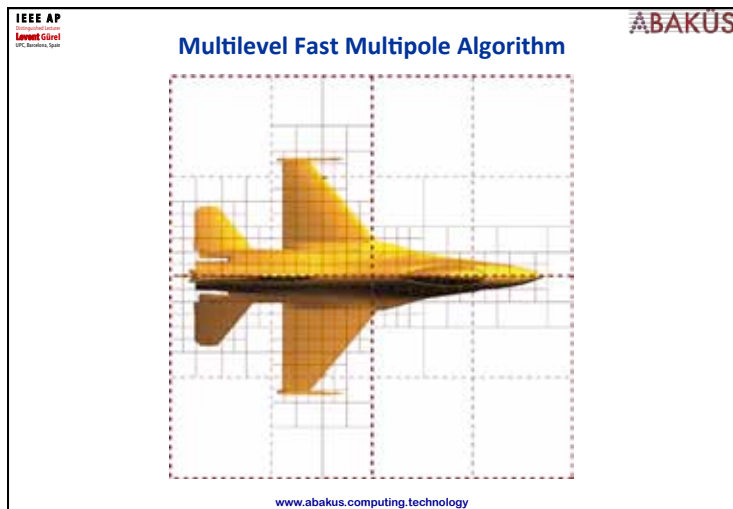
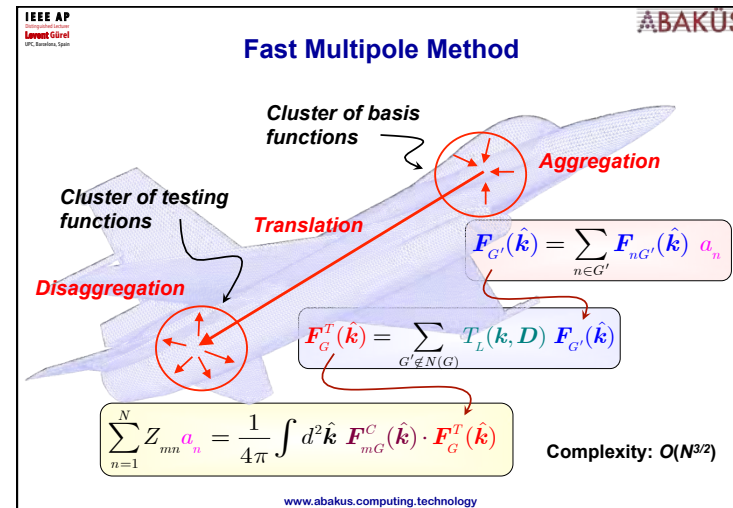
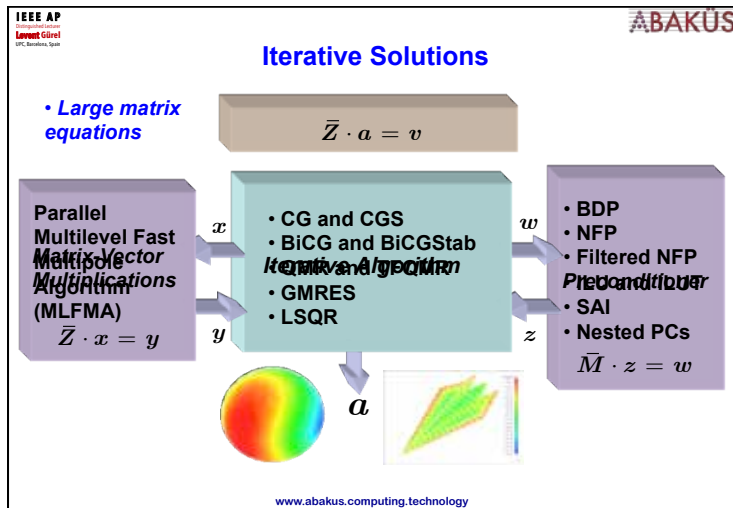
System of Linear Equations

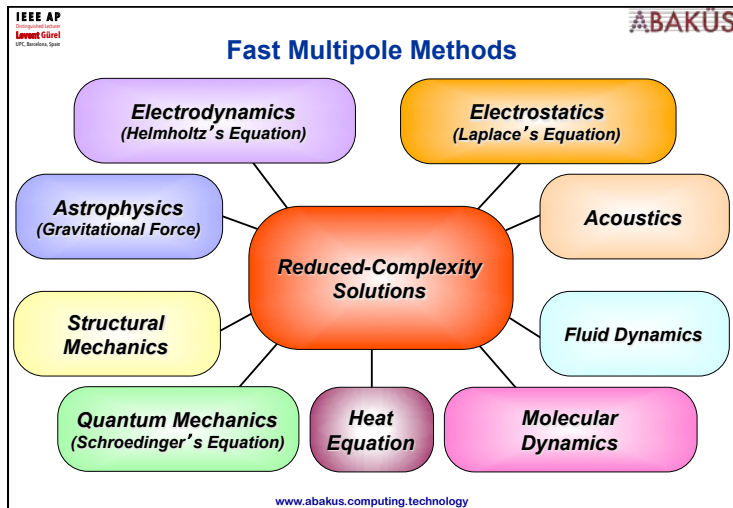
$$Z \cdot a = v$$

Algorithmic Complexity

- Gaussian Elimination: $O(N^3)$
- Cramer Rule: $O(N!), O(N^3)$
- Iterative Methods: $O(kN^2)$
- Fast Algorithms: $O(N \log N), O(N)$

www.abakus.computing.technology

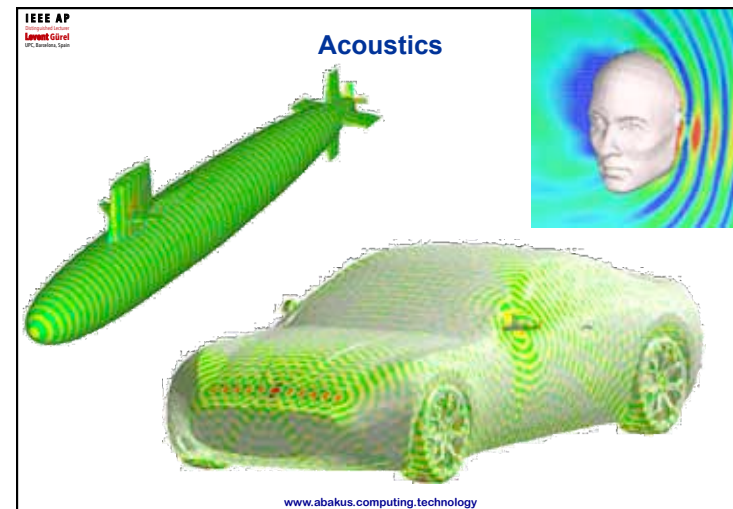
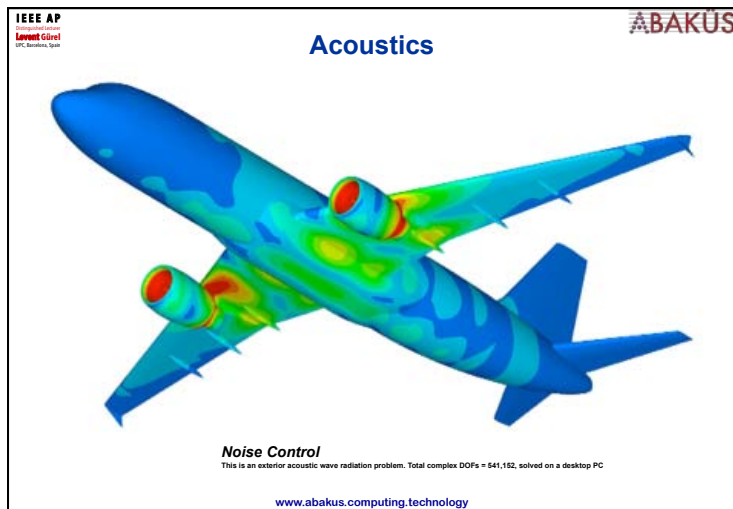




Acoustics and Elastics

- Y. H. Chen, W. C. Chew, and S. Zeroug, "Fast multipole method as an efficient solver for 2D elastic wave surface integral equations," Computational Mechanics, vol. 20, pp. 495-506, 1997.
- M. S. Tong, W. C. Chew, and M. J. White, "Multilevel fast multipole algorithm for acoustic wave scattering by truncated ground with trenches," Journal of Acoustic Society of America, vol. 123, no. 5, pp. 2513-2521, 2008.
- M. S. Tong and W. C. Chew, "Multilevel fast multipole algorithm for elastic wave scattering by large 3D objects," Journal of Computational Physics, vol. 228, no. 3, pp. 921-932, 2009.

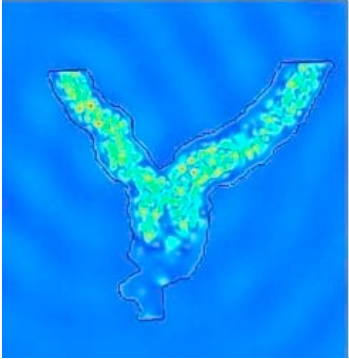
www.abakus.computing.technology



IEEE AP
Lorentz Gürel
UPC Barcelona, Spain

ABAKUS

Seismic Wave Propagation



S. Chaillat, J.F. Semblat, M. Bonnet, A preconditioned 3-D multi-region fast multipole solver for seismic wave propagation in complex geometries. Communications in Computational Physics (special issue WAVES), 2009, Vol. 11, 264-676, 2012.

www.abakus.computing.technology

IEEE AP
Lorentz Gürel
UPC Barcelona, Spain

ABAKUS

Schrödinger's Equation

- **Volumetric fast multipole method for modeling Schrödinger's equation**

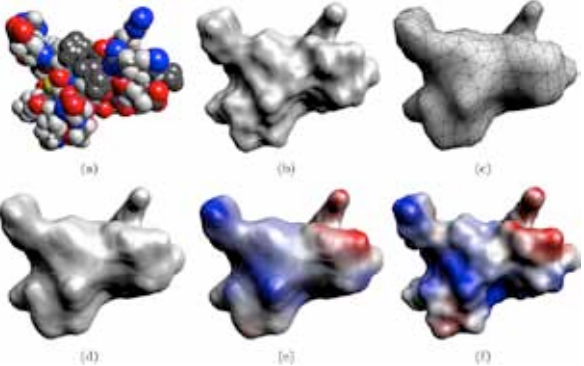
Zhiqin Zhao, Narayan Kovvali, Wenbin Lin, Chang-Hoi Ahn, Luise Couchman, Lawrence Carin
Department of Electrical and Computer Engineering, Duke University, Durham, NC 27708-0291, USA; Naval Research Laboratory, Washington, DC, USA; School of Electronic Engineering, University of Electronic Science and Technology of China, Chengdu, China, Journal of Computational Physics (Impact Factor: 2.14), 06/2007; DOI: 10.1016/j.jcp.2006.11.003

www.abakus.computing.technology

IEEE AP
Lorentz Gürel
UPC Barcelona, Spain

ABAKUS

Molecular Electrostatics



AN EFFICIENT HIGHER-ORDER FAST MULTIPOLE BOUNDARY ELEMENT SOLUTION FOR POISSON-BOLTZMANN BASED MOLECULAR ELECTROSTATICS
Chandragiri Rajaji, Shun-Chuan Chen, and Alexander Rand
SIAM J Sci Comput, Jan 1, 2011, 33(2): 828-848.

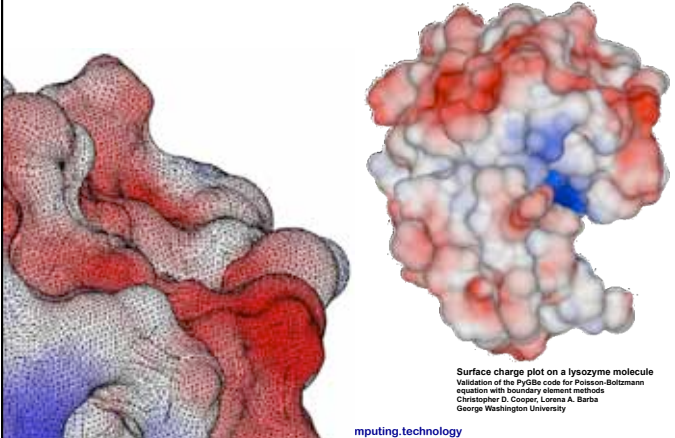
(a) Molecular model of a protein (PDB id: 1PHE, 404 atoms). (b) The van der Waals surface of the protein which models the molecule as a union of beads. (c) The variational molecular surface gives a smooth approximation of the van der Waals surface. (d) The variational surface is then triangulated and then smoothed to produce a smaller mesh. (e) The smoothed mesh contains a 500 triangles. (f) The approximate volume molecular surface (AVMS) for a smooth surface used the triangular mesh. (g) Electrostatic potential computed using the 1,000 patch AVMS. (h) Electrostatic potential using an AVMS with 74,412 patches. The surface is 46 nm² (area covered by the electrostatic potential), ranging from -13.8 kT (red level) to 13.8 kT (blue level).

www.abakus.computing.technology

IEEE AP
Lorentz Gürel
UPC Barcelona, Spain

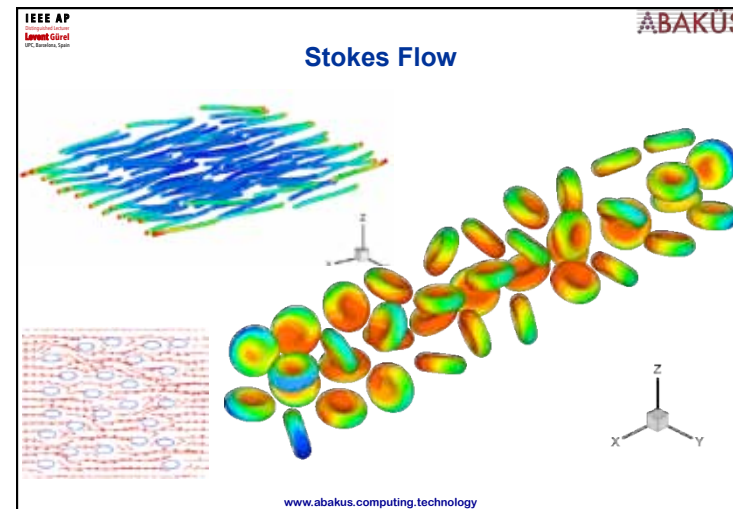
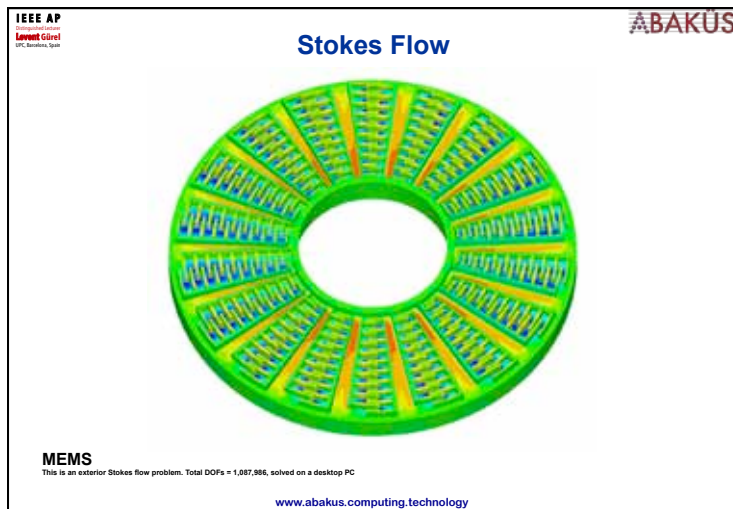
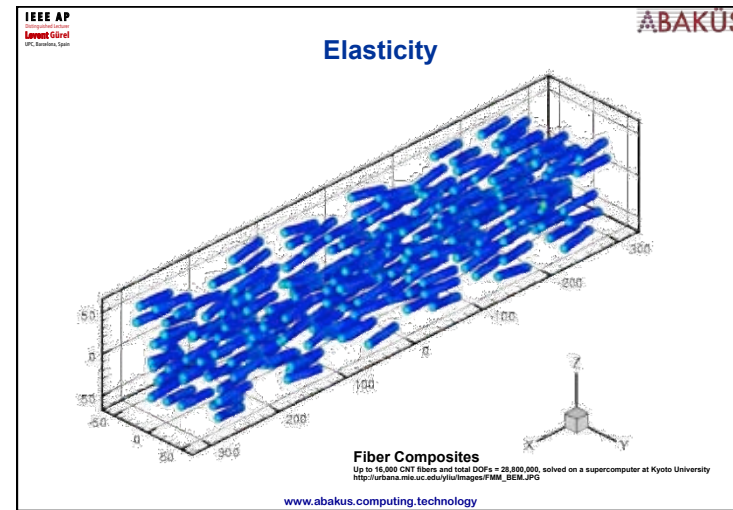
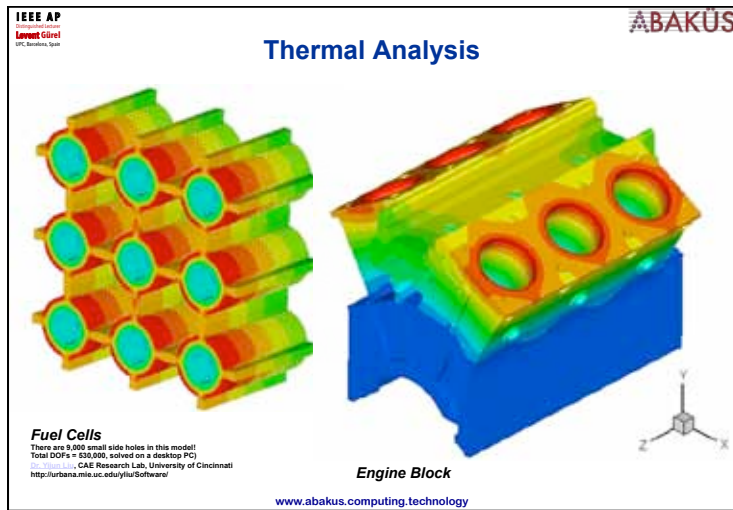
ABAKUS

Biomolecular Electrostatics



Surface charge plot on a lysozyme molecule
Validation of the PyGBe code for Poisson-Boltzmann equation with boundary element methods
Christopher D. Cooper, Lorena A. Barba
George Washington University

www.abakus.computing.technology



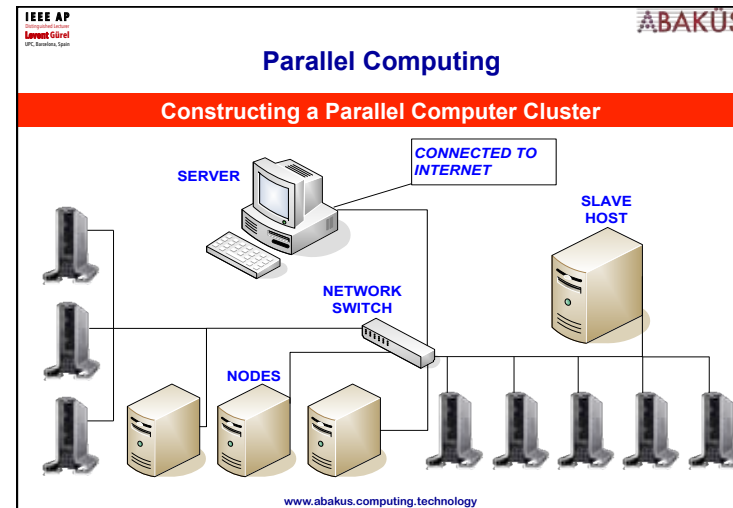
IEEE AP **Lluís Górriz** UPC Barcelona, Spain **ABAKUS**

Books





www.abakus.computing.technology



IEEE AP **Lluís Górriz** UPC Barcelona, Spain **ABAKUS**

Parallel Computing

Constructing Parallel Computer Clusters

64-Core Cluster

8 nodes

Per node: Two Intel Xeon 5145 3 GHz Processors

Total of 64 cores

Per node: 32 GB DDR2-667 533 MHz RAM

Total of 256 GB of RAM

Network: Infiniband

136-Core Cluster

Per node: Two Intel Xeon 5472 3 GHz Quad-Core Processors

Total of 136 cores

Per node: 4 GB DDR2-667 533 MHz RAM

Total of 544 GB of RAM

Network: Infiniband

Not in www.top500.org!!!

www.abakus.computing.technology

IEEE AP
Lluís Gómez
UPC Barcelona, Spain

ABAKUS

What is the Main Source of Efficiency?

N Unknowns	$O(N^3)$ Gaussian Elimination	$O(N^2)$ Iterative MOM (MVM)	$O(N^{3/2})$ Single-Level FMM	$O(N \log N)$ Multi-Level FMM
1000	1 s	2 s	4 s	8 s
10^6	32 years	23 days	35 h	7 h
10^7	32 K years	6.3 years	46 days	89 h
10^8	32 M years	630 years	4 years	46 days
10^9	32 G years	63 K years	127 years	1.5 years (555 days)

www.abakus.computing.technology

IEEE AP
Lluís Gómez
UPC Barcelona, Spain

ABAKUS

53 Million Unknowns

Sphere with radius of 120λ and diameter of 240λ

November 2007

53,112,384 Unknowns

www.abakus.computing.technology

IEEE AP
Lluís Gómez
UPC Barcelona, Spain

ABAKUS

69 Million Unknowns

Sphere with radius of 150λ and diameter of 300λ

December 2007

69,177,600 Unknowns

www.abakus.computing.technology

IEEE AP
Lluís Gómez
UPC Barcelona, Spain

ABAKUS

85 Million Unknowns

Sphere with radius of 150λ and diameter of 300λ

January 2008

Scattering results are compared to analytical values to demonstrate the accuracy of the numerical solution.

85,148,160 Unknowns

www.abakus.computing.technology

IEEE AP
Luis M. Górriz
UPC Barcelona, Spain

Intel Pamphlet on the World Record



ABAKUS

Case Study
Intel Core™ Xeon® processor E5-2600 series
Intel® Xeon® processor E5-2600 series

Breakthrough in Scientific Computing: BiLCEM Sets World Record in Computational Electromagnetics

Bilkent University opens the door to a secret universe thanks to Quad-Core Intel® Xeon® processor E5-2600 series

Bilkent University in Ankara, Turkey, is one of the world's leading research universities and home to the Bilkent University Computational Electromagnetics Research Center (BILCEM), a globally respected institute specializing in the solution of the largest and most difficult problems in computational electromagnetics. BILCEM's research and analysis use rigorous, iterative, and more often iterative, through computers that typically derive millions of unknowns, which is extremely challenging. Being aware of CPU problems can result in the need for parallel computing. To make significant advances in the field.

Available at www.com.bilkent.edu.tr

BILCEM

www.abakus.computing.technology

IEEE AP
Luis M. Górriz
UPC Barcelona, Spain

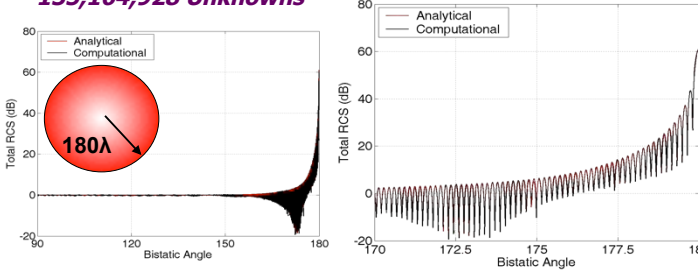
135 Million Unknowns

August 2008

Sphere with radius of 180λ and diameter of 360λ

Scattering results are compared to analytical values to demonstrate the accuracy of the numerical solution.

135,164,928 Unknowns



www.abakus.computing.technology

IEEE AP
Luis M. Górriz
UPC Barcelona, Spain

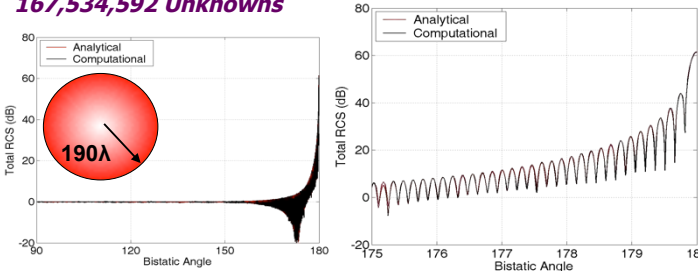
167 Million Unknowns

August 2008

Sphere with radius of 190λ and diameter of 380λ

Scattering results are compared to analytical values to demonstrate the accuracy of the numerical solution.

167,534,592 Unknowns



www.abakus.computing.technology

IEEE AP
Luis M. Górriz
UPC Barcelona, Spain

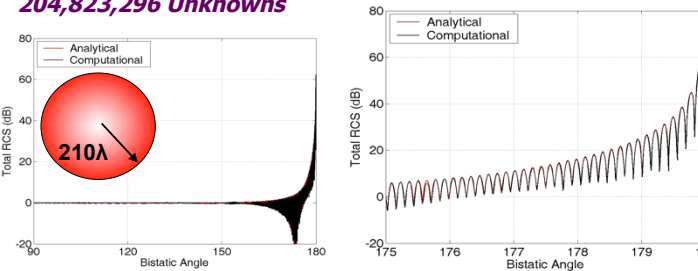
205 Million Unknowns

September 2008

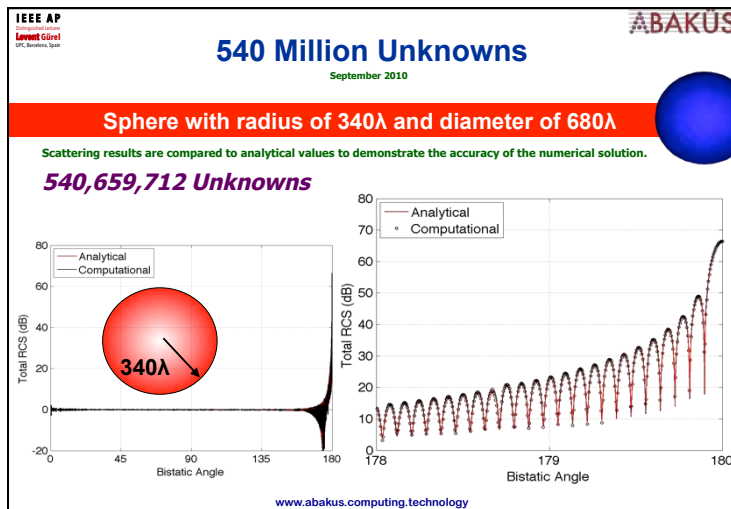
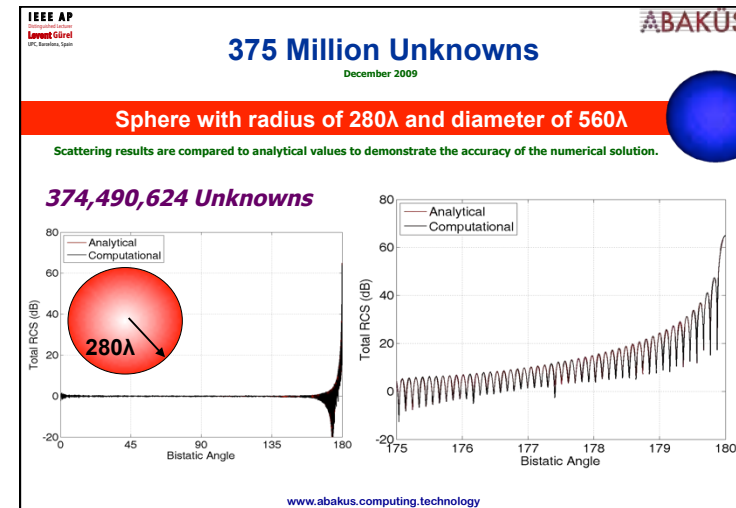
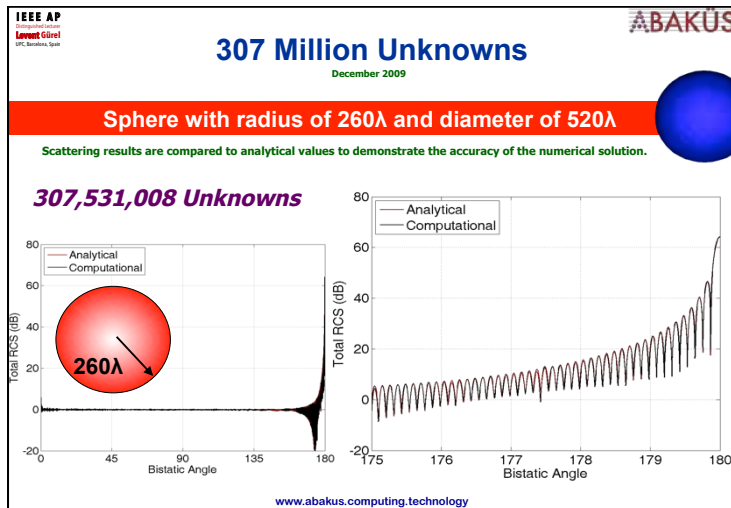
Sphere with radius of 210λ and diameter of 420λ

Scattering results are compared to analytical values to demonstrate the accuracy of the numerical solution.

204,823,296 Unknowns



www.abakus.computing.technology



IEEE AP
Lluís Górriz
UPC Barcelona, Spain

ABAKUS

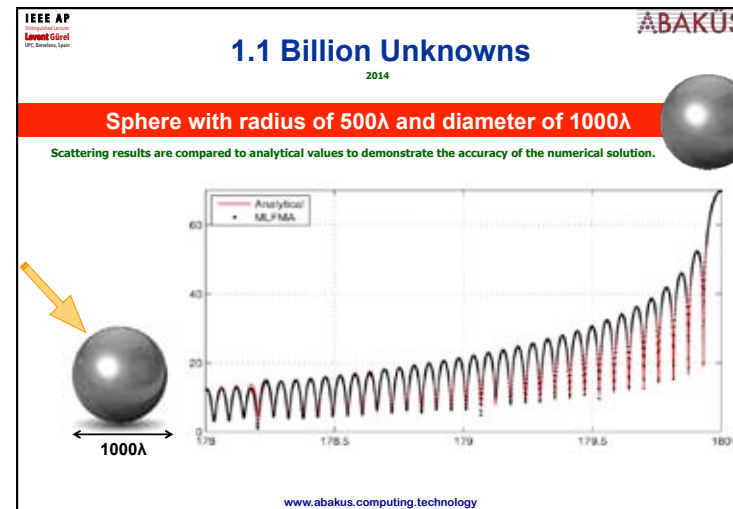
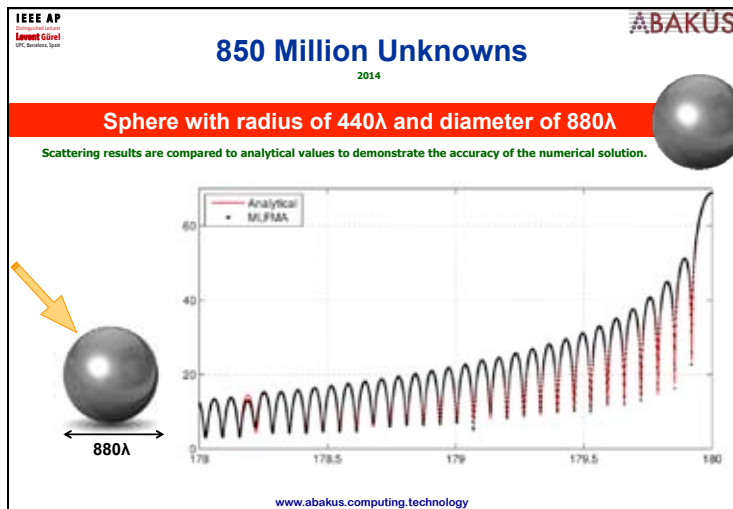
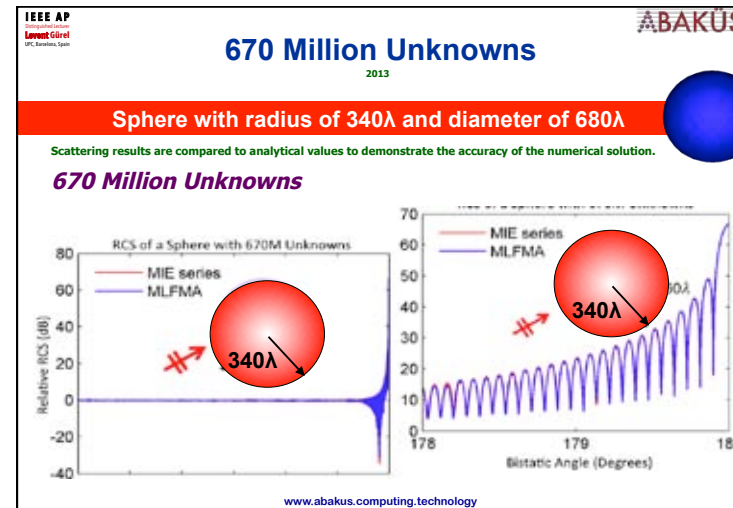
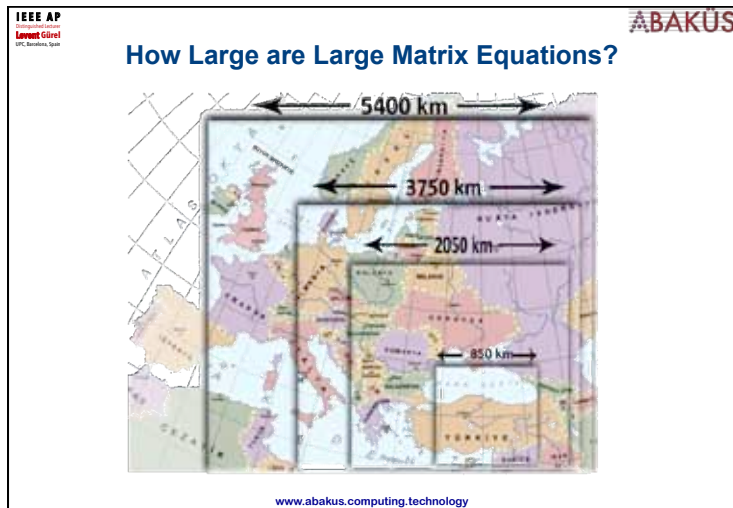
How Large are Large Matrix Equations?

Each element of the matrix is a complex number with real and imaginary parts

$7.654321E+02$
 $+ j 1.234567E-03$

If we could fit each element of the matrix in a square of 1 cm by 1 cm...

www.abakus.computing.technology

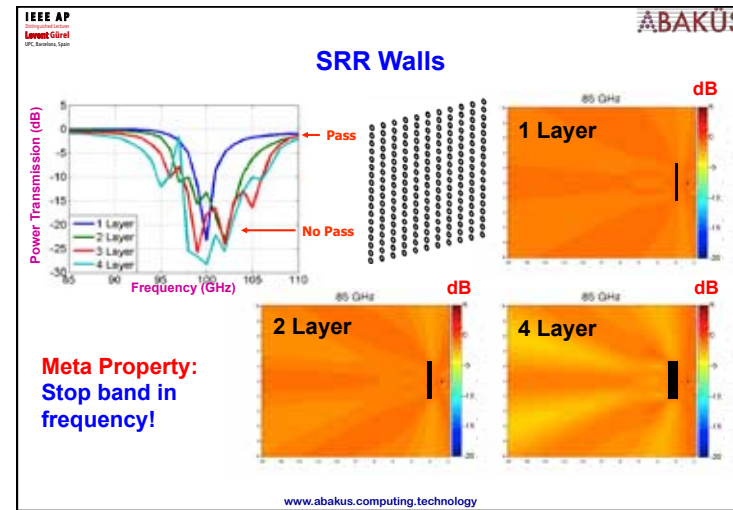


IEEE AP
Lluís Gómez
UPC Barcelona, Spain

ABAKUS

Nanomaterials: Metamaterials Split-Ring Resonators

www.abakus.computing.technology



IEEE AP
Lluís Gómez
UPC Barcelona, Spain

ABAKUS

Special Configurations

Closed-Ring Resonators (CRRs)

Thin Wire Array (TWA)

All pass!

No pass!

www.abakus.computing.technology

IEEE AP
Lluís Gómez
UPC Barcelona, Spain

ABAKUS

Composite Metamaterial (CMM)

Split-Ring Resonators (SRRs)

Thin Wire Array (TWA)

www.abakus.computing.technology

